

## 7.6 Decision Nonlinearities

7.6.1

- In Sections 7.4 and 7.5, we modified the iterative linear receivers by incorporating the  $\text{dec}(x)$  nonlinearity between iterations, hoping for better cancellation and closer approach to ML.

- Here we look at  $\text{dec}(x)$  in more detail and generalize it, to prepare for the methods of Sections 7.7 and 7.8

- We have been using

$$\text{dec}(x) = \underset{b \in \mathcal{Q}}{\text{argmin}} |x - b|$$

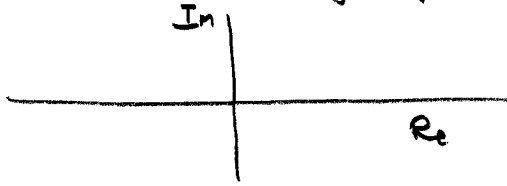
Choose the constellation point nearest  $x$ .

- If no constellation mapping imposed, as in the iterative linear methods of Sections 7.1, 7.2, then  $b \in \mathcal{C}$ , and min is achieved with  $b = x$ . Hence

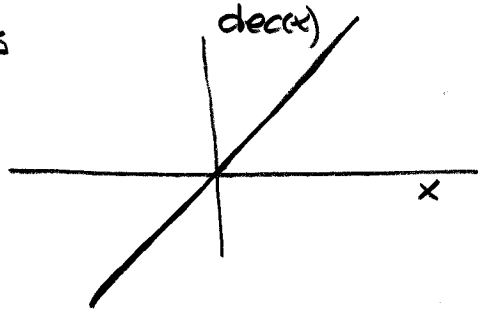
$$\text{dec}(x) = x$$

so we didn't use the  $\text{dec}$  function in those sections.

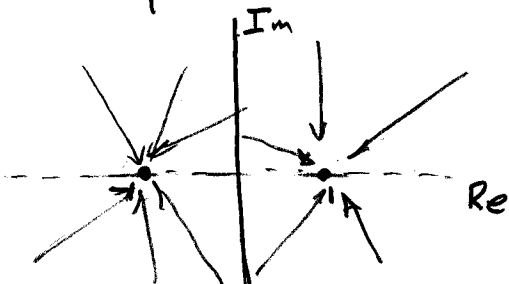
- In this case, the  $\text{dec}(x)$  function is a unity mapping of the plane to itself



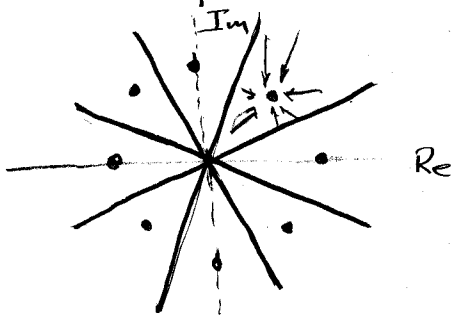
- If  $x$  is always real, then the I/O of the function is



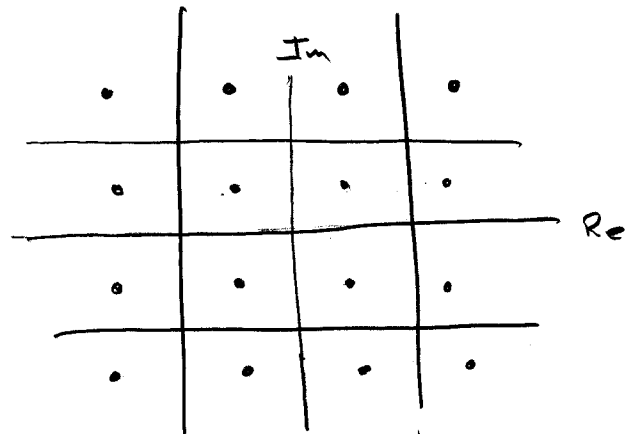
- If we have a discrete constellation, then  $\text{dec}(x)$  incorporates classical decision boundaries.



All points  $x$  are mapped onto the constellation point in their half plane

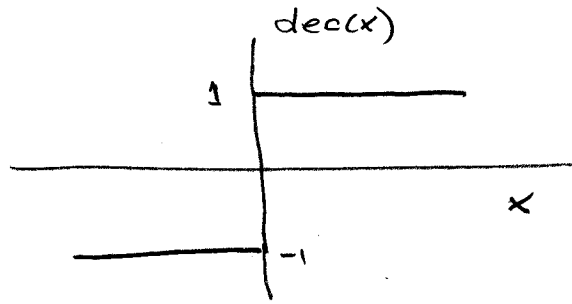


8 PSK

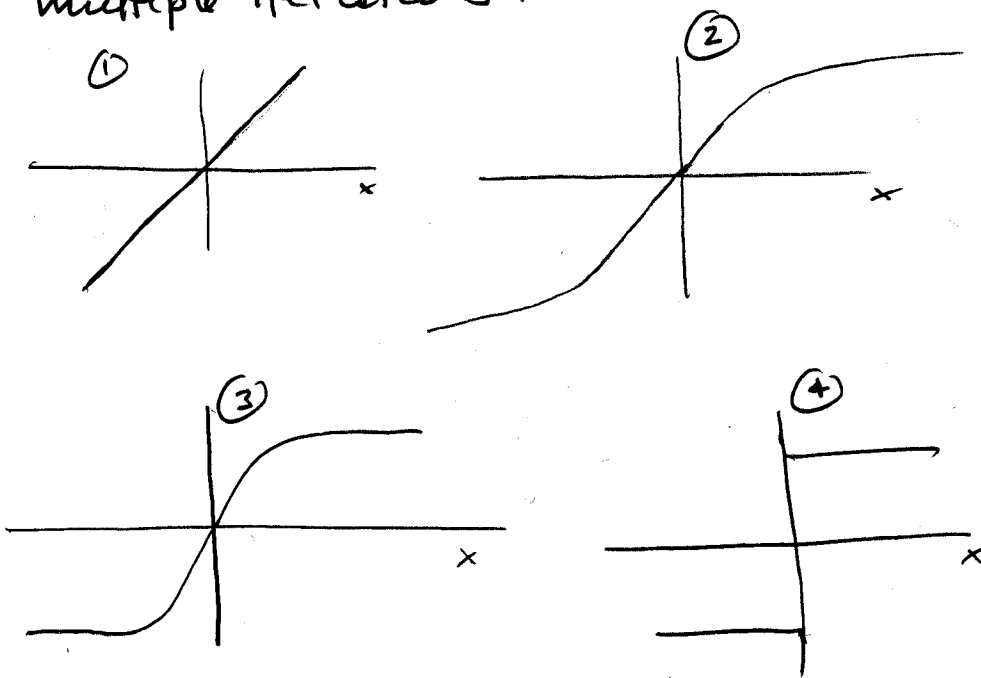


16 QAM

- If  $x$  is always real and its BPSK modulation, <sup>T. Le. 3</sup>  
then the I/O relation is

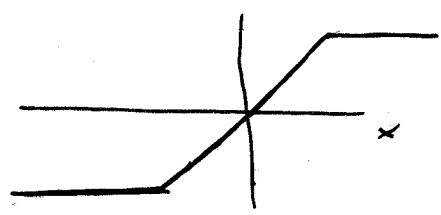


- The use of a decorrelator as the first stage of PIC (or SIC, for that matter) followed by the  $\text{sgn}$  hard limiter as second stage suggests intermediate soft nonlinearities for multiple iterations.



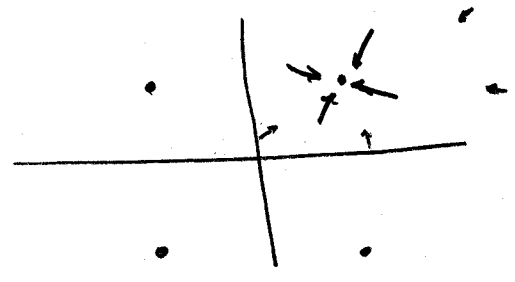
Various families of functions will do this, eg  $\tanh'(ax)$

Another candidate is

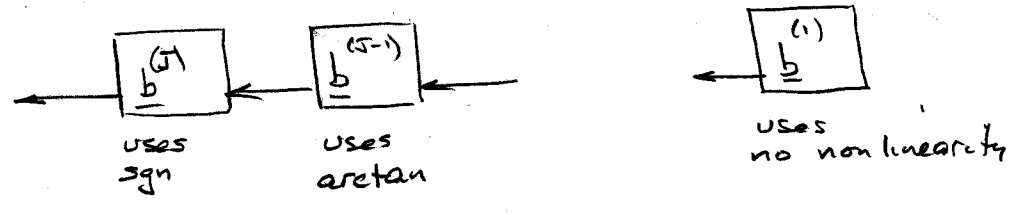


clipped soft nonlinearity

- For 2-D constellations, we could construct varying degrees of "pull" from the constellation points



- The pipeline structure can use harder nonlinearities with each iteration unit



- But it all seems quite ad hoc. We need a more analytical approach to guide us.