# SIMON FRASER UNIVERSITY SCHOOL OF ENGINEERING SCIENCE

# Summer 2012 ENSC 320: ELECTRIC CIRCUITS II

# Midterm Examination Monday, July 16, 2012

Duration: 110 minutes. Attempt all four problems. Questions are not equally weighted. Closed book and closed notes. Calculators, PDAs, laptops, and wireless phones are not permitted. Use a ball-point pen for writing the exam (no pencils, please).

### 1. Laplace Transform Analysis: Circuit Applications (20 points)

Consider the switched RLC circuit shown in Figure 1. Suppose the switch has been in position A for a long time and moves to point B at t = 0. Suppose  $v_{in}(t) = 50$  V.

- Find  $i_L(t)$  and  $v_C(t)$  at  $t=0^-$ .
- Find  $v_C(t)$  for t > 0.
- Sketch  $v_C(t)$  for  $t \geq 0$ .

### 2. Laplace Transform Analysis: Transfer Function Applications (30 points)

Consider the circuit shown in Figure 2, where  $R_1 = 50 \Omega$ ,  $R_2 = 200 \Omega$ , and C = 2.5 mF.

- Find the circuit's transfer function.
- Let  $v_{in}(t) = 10e^{-2t}u(t) V$  and  $v_c(0_-) = 4 V$ .
  - Use Laplace transform to find the complete response of the circuit by first finding the zero-state response and the zero-input response.
  - Identify the circuit's forced response and natural response.
  - Identify the circuit's steady-state response and transient response.
- Let  $v_{in}(t) = 10e^{-10t}u(t) V$  and  $v_c(0_-) = 0 V$ . Is the forced response well defined? Justify your answer.

#### 3. The Convolution Method (20 points)

Consider the circuit shown in Figure 3. Suppose that the input excitation is  $v_{in}(t) = e^{-a|t|}$  V, where  $a \neq 1$  and a > 0.

- Find the circuit's impulse response.
- Determine the response  $v_{out}(t)$  for all t.

# 4. Resonant and Bandpass Circuits (30 points)

For the bandpass circuit shown in Figure 4:

- Find the transfer function  $H(s) = I_L(s)/V_{in}(s)$ .
- Find  $\omega_m$ ,  $H_m$ , and  $B_{\omega}$ .

