

SIMON FRASER UNIVERSITY  
SCHOOL OF ENGINEERING SCIENCE

Summer 2012  
ENSC 320: ELECTRIC CIRCUITS II

Midterm Examination  
Monday, June 25, 2012

*Duration: 110 minutes. Attempt all four problems. Questions are not equally weighted.  
Closed book and closed notes. Calculators, PDAs, laptops, and wireless phones are not  
permitted. Use a ball-point pen for writing the exam (no pencils, please).*

**1. Second-Order Linear Circuits (30 points)**

The switch in the circuits shown in Figure 1 is closed at  $t = 0$ . The dependent source gain  $k$  is a positive constant.

- Find the voltage response  $v_c(t)$ .
- Find the range of  $k$  such that the voltage response  $v_c(t)$  is over-damped.
- Find the response  $v_c(t)$  for the value of  $k$  that makes the circuit critically damped.

**2. Laplace Transform: Basics (15 points)**

- Find Laplace transform of the signal sketched in Figure 2.
- Find the inverse Laplace transform of the following function of  $s$ :

$$F(s) = \frac{4s^2 + 7s + 1}{s(s + 1)^2}.$$

(Use simplifications and the transform properties to simplify calculations.)

- Apply the initial-value and final-value theorems to the transform pair.

**3. Laplace Transform Analysis: Circuit Applications (20 points)**

A series RLC circuit is shown in Figure 3. Circuit parameters are:  $R = 4\Omega$ ,  $L = 1H$ , and  $C = 0.2F$ . Use Laplace transform to find the circuit's:

- impulse response
- step response.

**4. Laplace Transform Analysis: Transfer Function Applications (35 points)**

Consider the circuit shown in Figure 4. Assume that the op-amp is ideal.

- Find transfer function  $H(s) = V_{out}/V_{in}$ .
- Find zeros and poles of  $H(s)$ .
- Find the magnitude and the phase of the frequency response.
- Plot the magnitude and the phase as functions of  $\omega$  and identify the type of the circuit.

Figure 1:

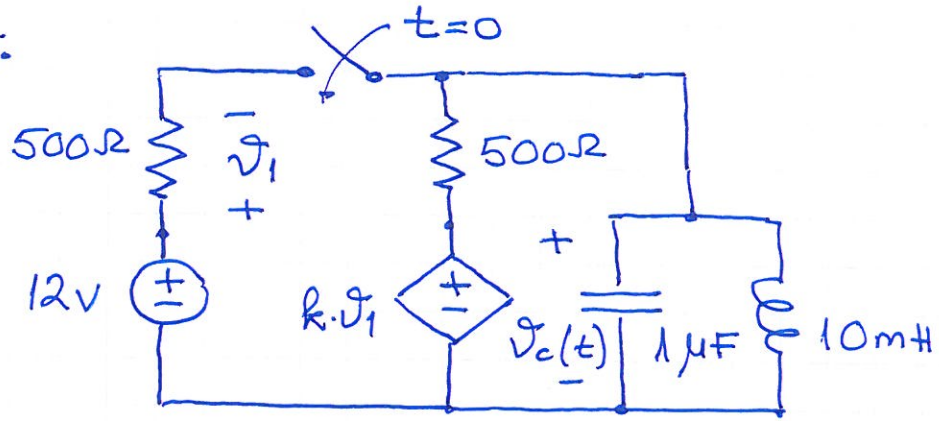


Figure 2:

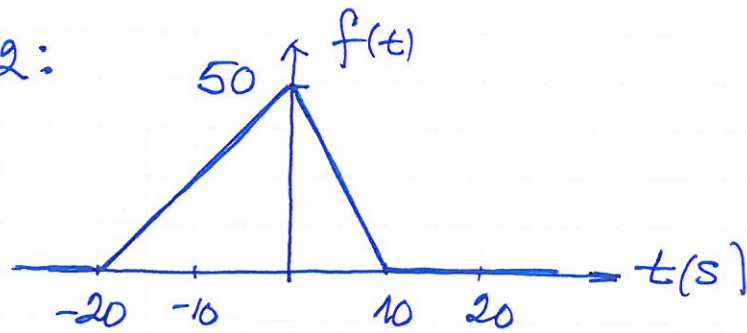


Figure 3:

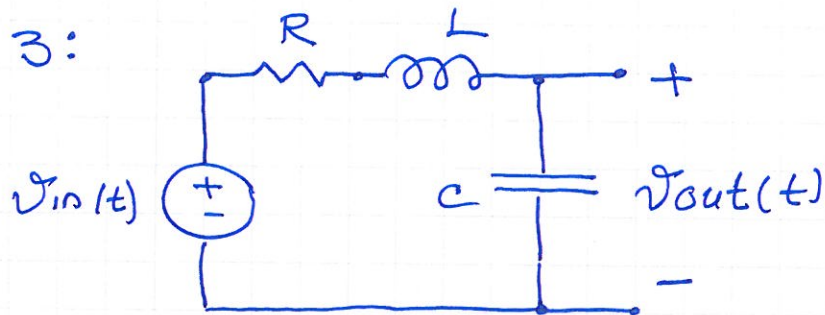


Figure 4:

