

MODELING AND CHARACTERIZATION OF TRAFFIC IN A PUBLIC SAFETY WIRELESS NETWORK

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Roadmap

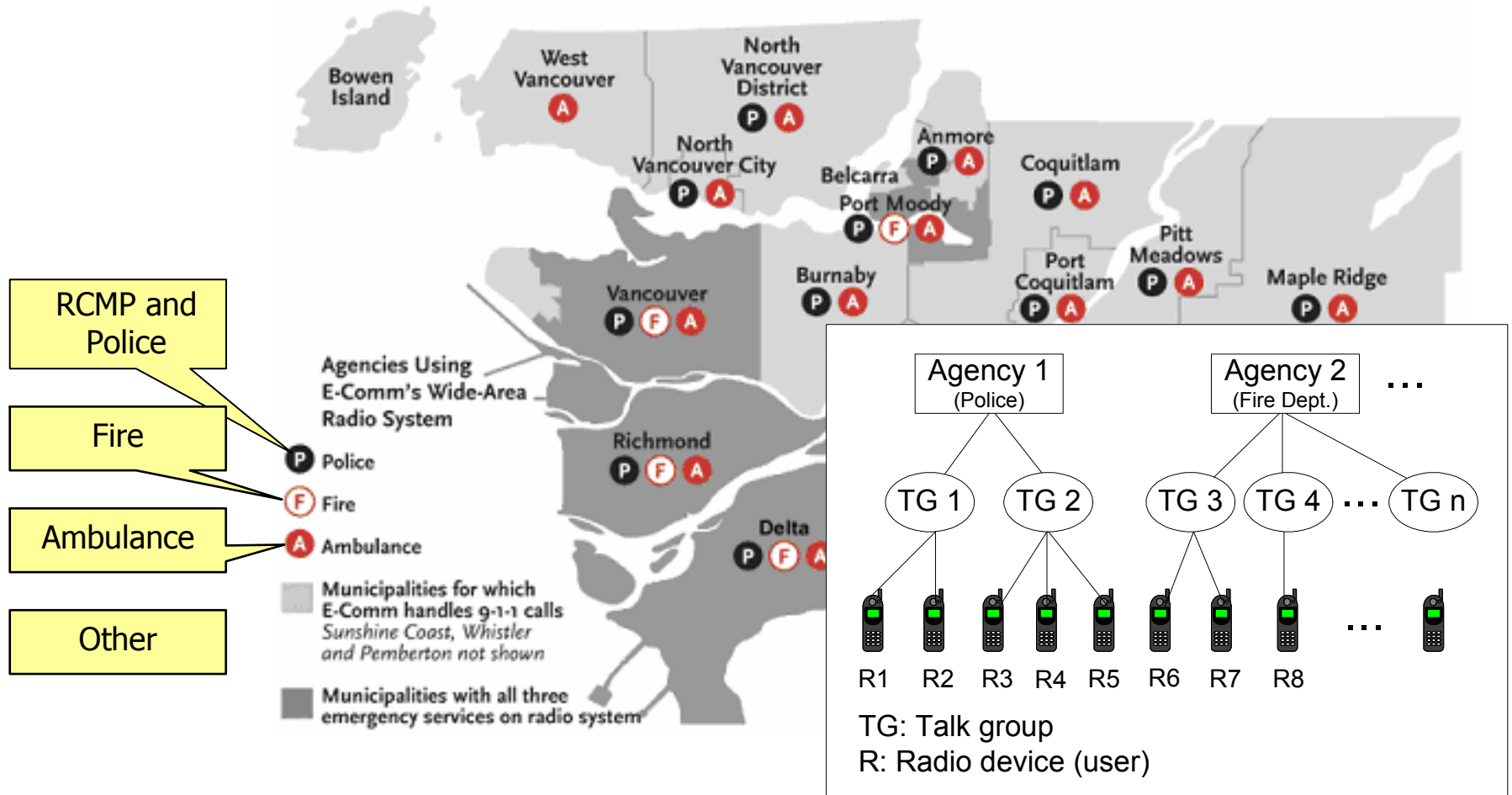
- Introduction
- Traffic data models
- OPNET simulation model
- Statistical concepts and analysis tools
- OPNET simulation results
- Statistical analysis of traffic data
- Conclusions and references



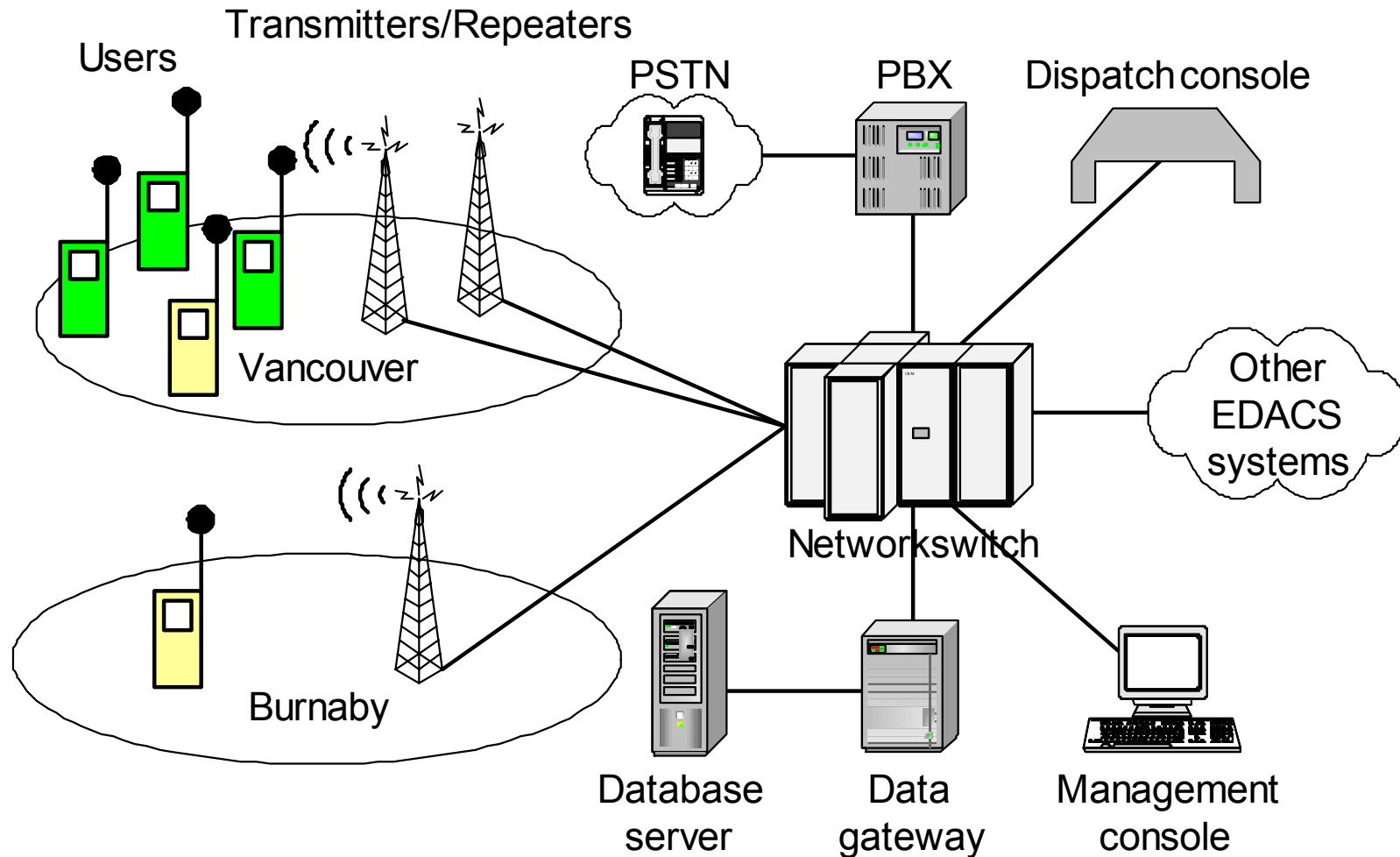
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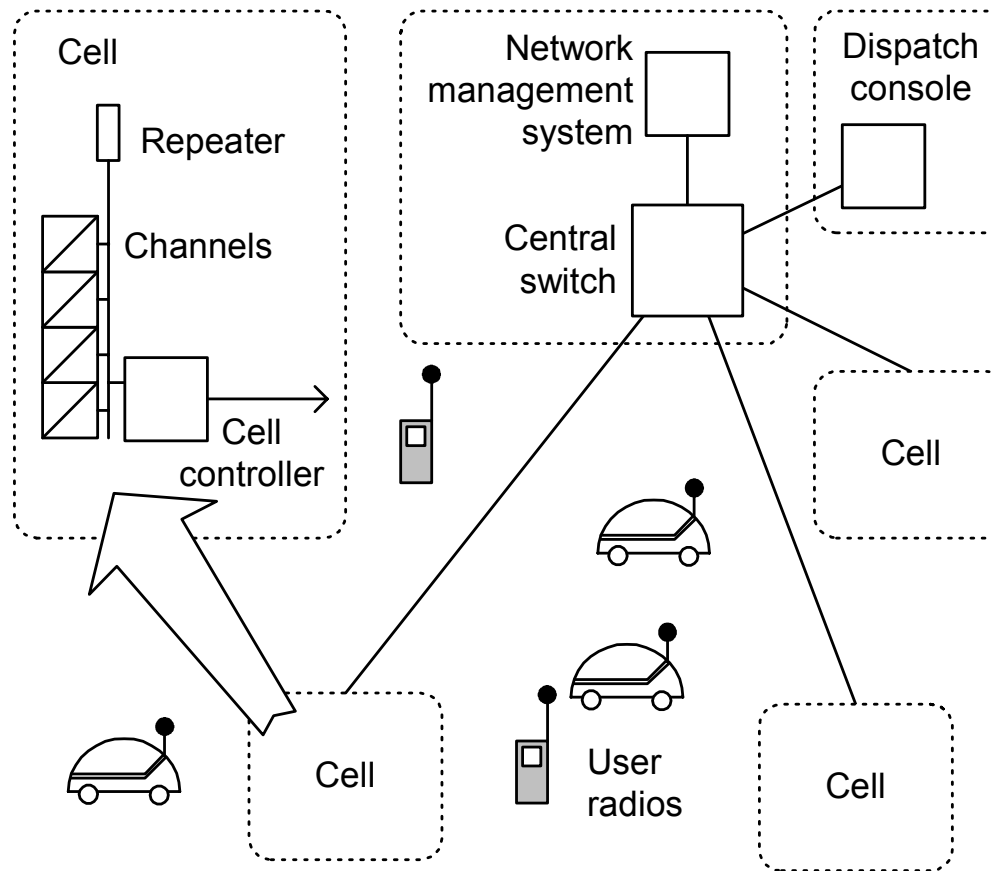
E-Comm network: coverage and user agencies



E-Comm network architecture



Structure of trunked radio systems





Network characteristics

- **EDACS:** Enhanced Digital Access Communications Systems
- **Simulcast:** repeaters covering one cell use identical frequencies
- **Trunking:** available frequencies in a cell are shared dynamically among mobile users
 - transmission trunking
 - message trunking
- **Cell capacity** (number of available frequencies in a cell):
 - one radio channel occupies one frequency
 - one call occupies one radio channel



Call establishment

- Users are organized in talk groups:
 - one-to-many type of conversations
- Push-to-talk (PTT) mechanism for network access:
 - user presses the PTT button
 - system locates other members of the talk group
 - system checks for availability of channels:
 - channel available: call established
 - all channels busy: call queued/dropped
 - user releases PTT:
 - call terminates



Erlang traffic models

Erlang B

$$P_B = \frac{\frac{A^N}{N!}}{\sum_{x=0}^N \frac{A^x}{x!}}$$

Erlang C

$$P_C = \frac{\frac{A^N}{N!} \frac{N}{N-A}}{\sum_{x=0}^{N-1} \frac{A^x}{x!} + \frac{A^N}{N!} \frac{N}{N-A}}$$

- P_B : probability of rejecting a call
- P_C : probability of delaying a call
- N : number of channels/lines
- A : total traffic volume



Erlang traffic models (2)

- Erlang B model assumes:
 - call holding time follows exponential distribution
 - blocked call will be rejected immediately
- Erlang C model assumes:
 - call holding time follows exponential distribution
 - blocked call will be put into a FIFO queue with infinite size



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Previous work

- Simulation:
 - OPNET
 - WarnSim
- Traffic prediction based on user clusters
 - Seasonal ARIMA model
- Statistical analysis of traffic

[1] N. Cackov, B. Vujičić, S. Vujičić, and Lj. Trajković, "Using network activity data to model the utilization of a trunked radio system," in *Proc. SPECTS*, San Jose, CA, July 2004, pp. 517–524.

[2] N. Cackov, J. Song, B. Vujicic, S. Vujicic, and Lj. Trajkovic, "Simulation and performance evaluation of a public safety wireless network: case study," *Simulation*, to appear.

[3] J. Song and Lj. Trajković, "Modeling and performance analysis of public safety wireless networks," in *Proc. IEEE IPCCC*, Phoenix, AZ, Apr. 2005, pp. 567–572.

[4] H. Chen and Lj. Trajković, "Trunked radio systems: traffic prediction based on user clusters," in *Proc. ISWCS*, Mauritius, Sept. 2004, pp. 76–80.

[5] D. Sharp, N. Cackov, N. Lasković, Q. Shao, and Lj. Trajković, "Analysis of public safety traffic on trunked land mobile radio systems," *IEEE J. Select. Areas Commun.*, vol. 22, no. 7, pp. 1197–1205, Sept. 2004.

[6] B. Vujičić, N. Cackov, S. Vujičić, and Lj. Trajković, "Modeling and characterization of traffic in public safety wireless networks," in *Proc. SPECTS 2005*, Philadelphia, PA, July 2005, pp. 14–223.



Traffic data

- 2001 data set:
 - 2 days of traffic data
 - 2001-11-1 to 2001-11-02 (110,348 calls)
- 2002 data set:
 - 28 days of continuous traffic data.
 - 2002-02-10 to 2002-03-09 (1,916,943 calls)
- 2003 data set:
 - 92 days of continuous traffic data
 - 2003-03-01 to 2003-05-31 (8,756,930 calls)



Sample of processed data: 2003-03-01

| No | Time (hh:mm:ss)(ms) | Call Duration (ms) | System Id | Channel Id | Caller | Callee |
|----|------------------------|--------------------------|--------------|---------------|--------|--------|
| 1 | 00:00:00 30 | 1340 | 1 | 12 | A | B |
| 6 | 00:00:00 489 | 1350 | 7 | 4 | A | B |
| 29 | 00:00:03 620 | 7550 | 2 | 7 | C | D |
| 31 | 00:00:03 760 | 7560 | 1 | 3 | C | D |
| 37 | 00:00:04 260 | 7560 | 7 | 6 | C | D |
| 38 | 00:00:04 340 | 7560 | 6 | 6 | C | D |



Traffic data used for OPNET simulations

- Timestamps and durations corresponding to single call differ due to discrepancies in records:
 - the smallest timestamp was chosen arbitrarily
 - the largest call duration (worst-case scenario) was used
- Original timestamp represents date and time of call start
 - in simulations: timestamp is difference between the original timestamp and arbitrary reference time
 - reference times: 0:00 on February 25, 2002 and 0:00 on March 10, 2003

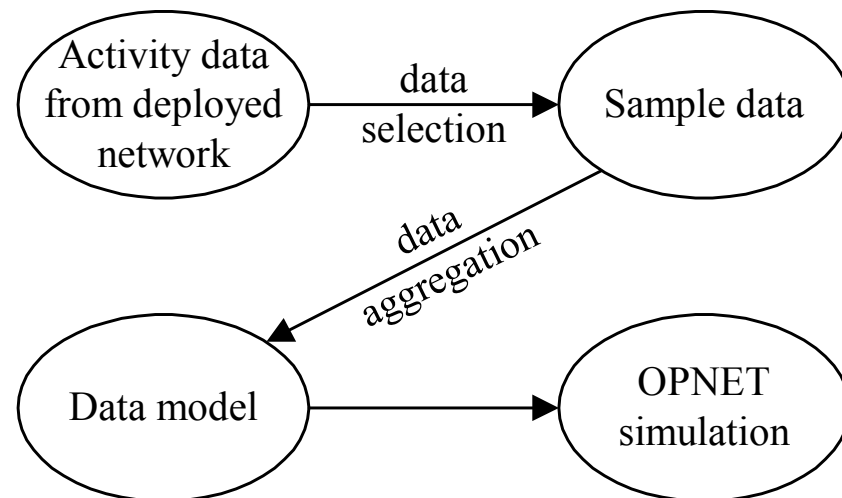
| Trace (dataset) | Time span |
|-----------------|---|
| 2002 | 0:00, February 25,2002 – 24:00, March 3, 2002 |
| 2003 | 0:00, March 10,2003 – 24:00, March 16, 2003 |

Data processing for OPNET model

| Timestamp | Duration (ms) | Caller | Callee | Cell |
|------------------------|---------------|--------|--------|------|
| 2003-03-20 0:00:10.639 | 4,870 | A | B | 4 |
| 2003-03-20 0:00:10.599 | 4,830 | A | B | 8 |
| 2003-03-20 0:00:10.529 | 4,860 | A | B | 9 |
| 2003-03-20 0:00:10.510 | 4,870 | A | B | 10 |

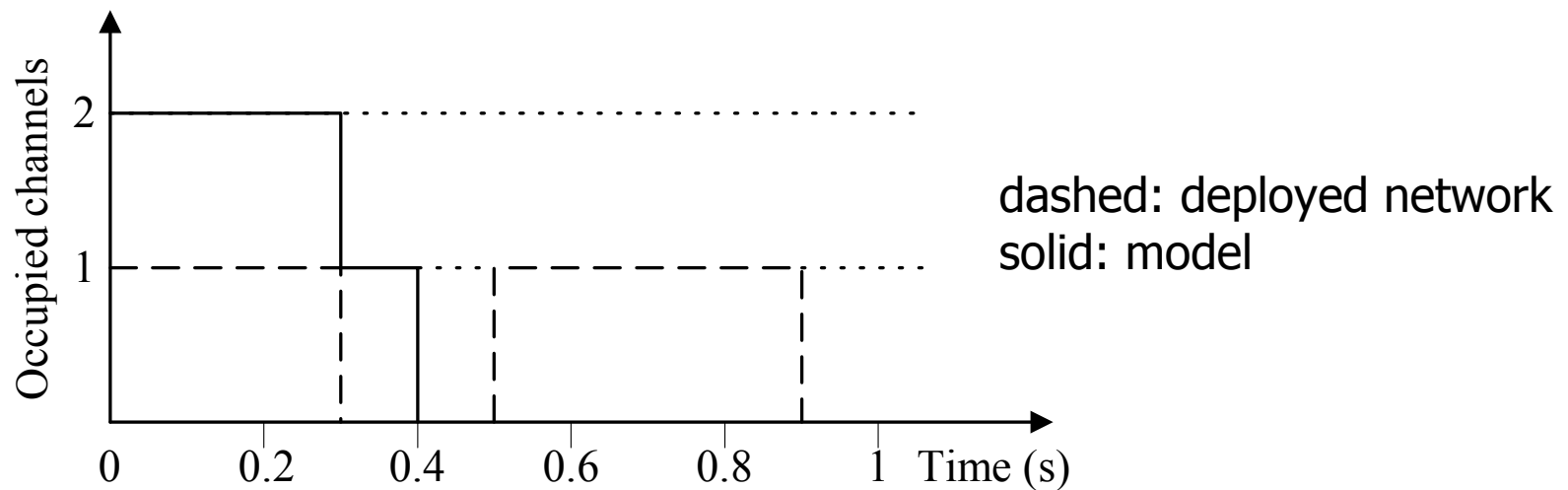


{10.510; 4,870; 4; 8; 9; 10}



Data discrepancies

- Coarse resolution of the timestamp
 - activity data: 10 ms
 - data model: 1 s
- Example:





Data discrepancies: 2003

- Overlapping usage of channels

| Timestamp | Duration (ms) | Cell | Channel |
|------------------------|---------------|------|---------|
| 2003-03-20 0:00:33.370 | 9,420 | 10 | 4 |
| ... | ... | ... | ... |
| 2003-03-20 0:00:42.769 | 4,290 | 10 | 4 |

- $0:00:42.769 < 0:00:33.370 + 9.420$
 - channel 4 in cell 10 is occupied by **two calls** at the same time!



Traffic data used for statistical modeling

- Records of network events:
 - established, queued, and dropped calls in the **Vancouver** cell
- Traffic data span periods during:
 - **2001, 2002, and 2003**

| Trace (dataset) | Time span | No. of established calls |
|-----------------|--------------------|--------------------------|
| 2001 | November 1–2, 2001 | 110,348 |
| 2002 | March 1–7, 2002 | 370,510 |
| 2003 | March 24–30, 2003 | 387,340 |

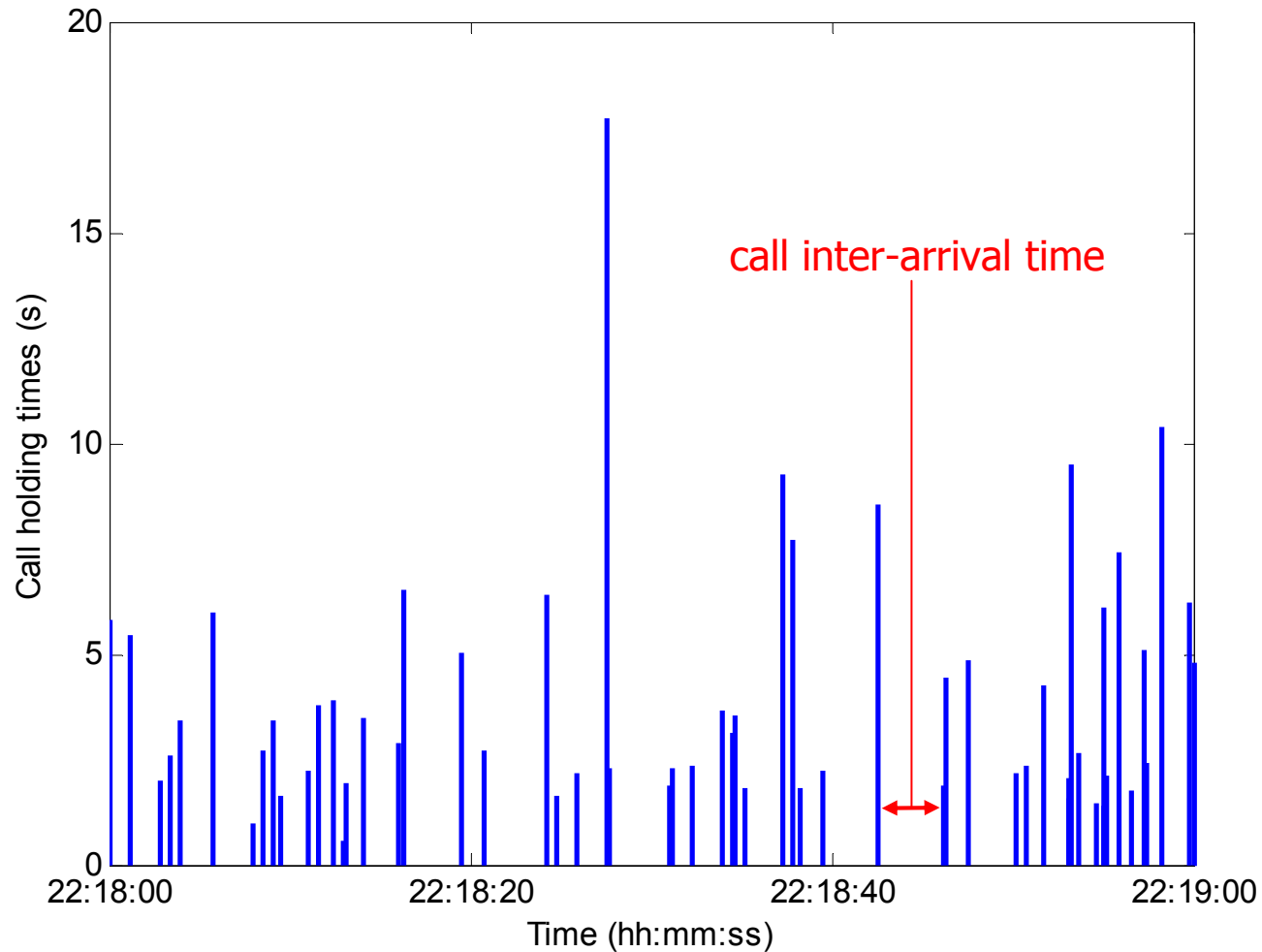


Hourly traces

- Call holding and call inter-arrival times from the **five busiest hours** in each dataset (2001, 2002, and 2003)

| 2001 | | 2002 | | 2003 | |
|---------------------------|-------|---------------------------|-------|---------------------------|-------|
| Day/hour | No. | Day/hour | No. | Day/hour | No. |
| 02.11.2001 15:00–16:00 | 3,718 | 01.03.2002 04:00–05:00 | 4,436 | 26.03.2003 22:00–23:00 | 4,919 |
| 01.11.2001 00:00–01:00 | 3,707 | 01.03.2002 22:00–23:00 | 4,314 | 25.03.2003 23:00–24:00 | 4,249 |
| 02.11.2001 16:00–17:00 | 3,492 | 01.03.2002 23:00–24:00 | 4,179 | 26.03.2003 23:00–24:00 | 4,222 |
| 01.11.2001 19:00–20:00 | 3,312 | 01.03.2002 00:00–01:00 | 3,971 | 29.03.2003 02:00–03:00 | 4,150 |
| 02.11.2001 20:00–21:00 | 3,227 | 02.03.2002 00:00–01:00 | 3,939 | 29.03.2003 01:00–02:00 | 4,097 |

Example: March 26, 2003



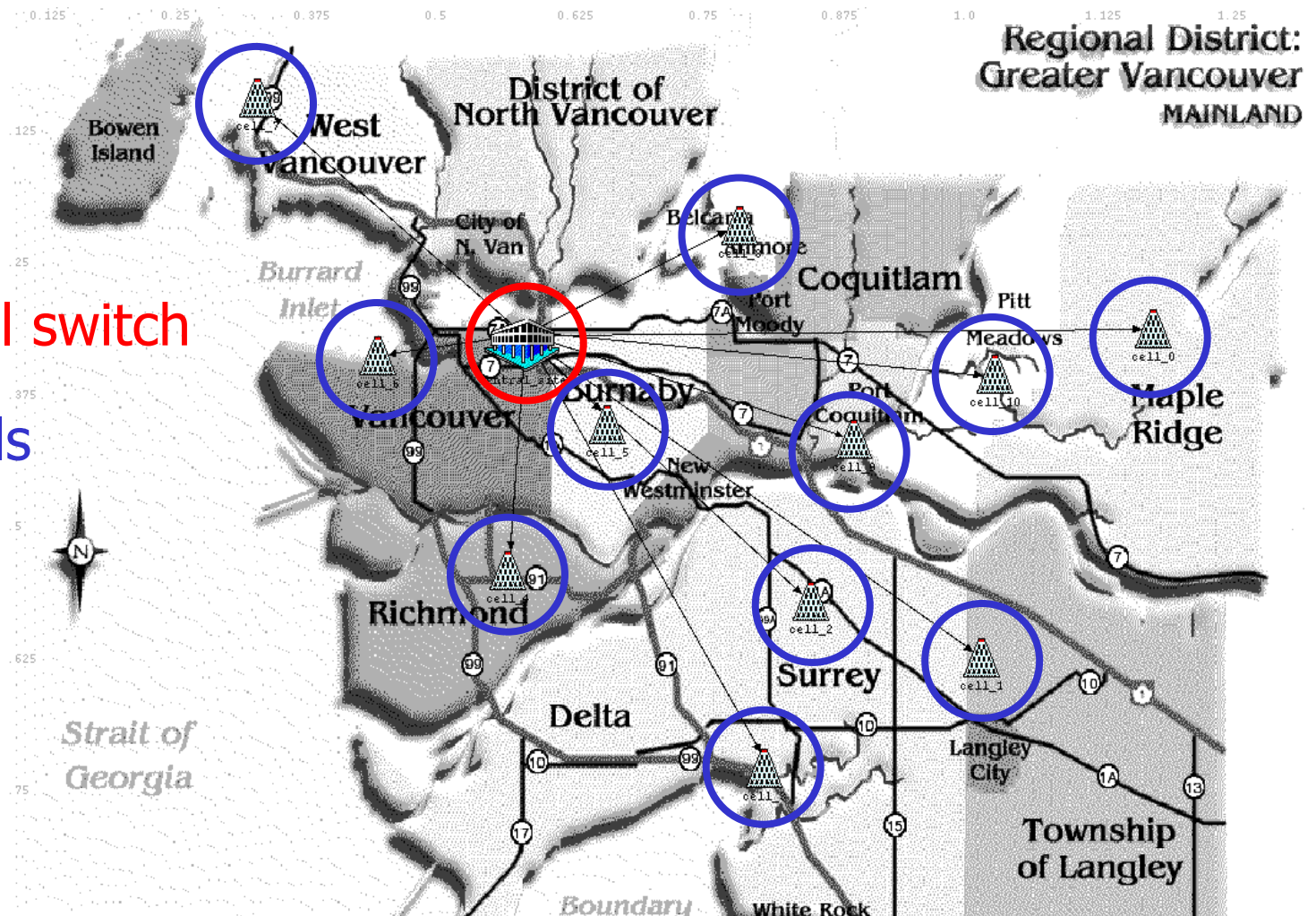


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Network model

- central switch
- 11 cells

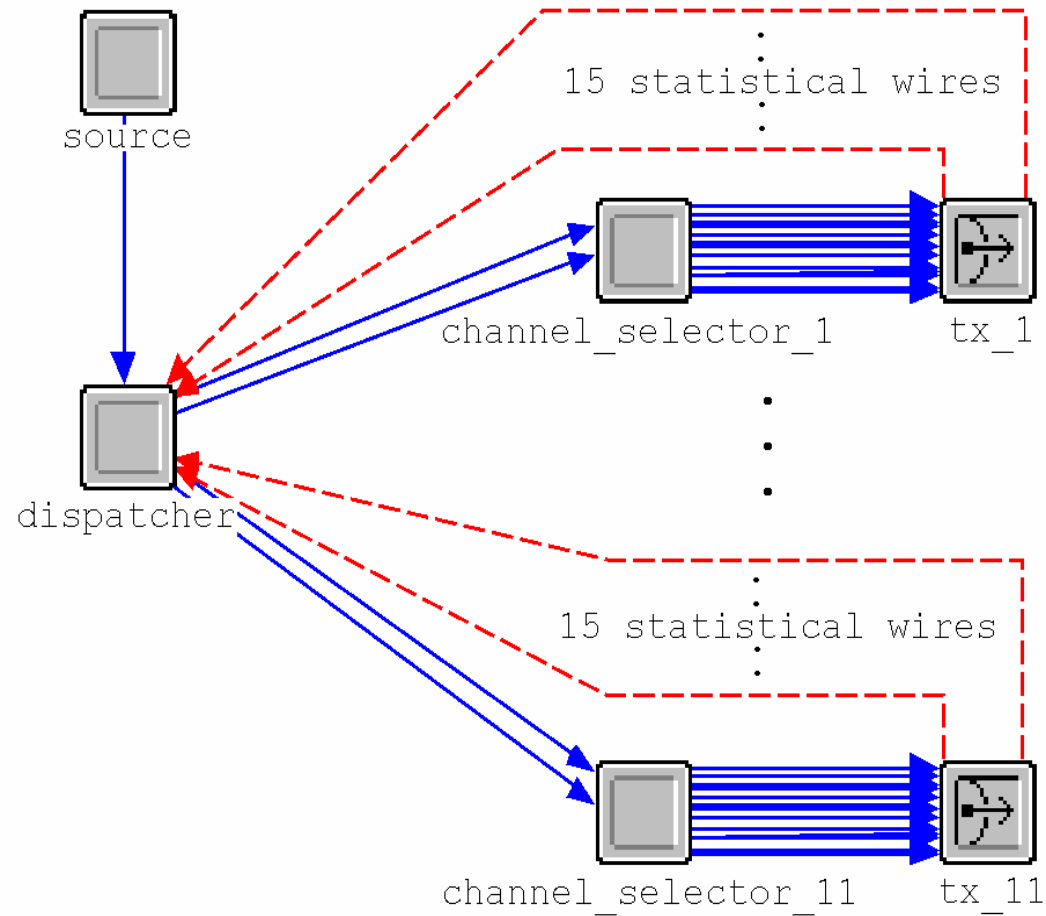




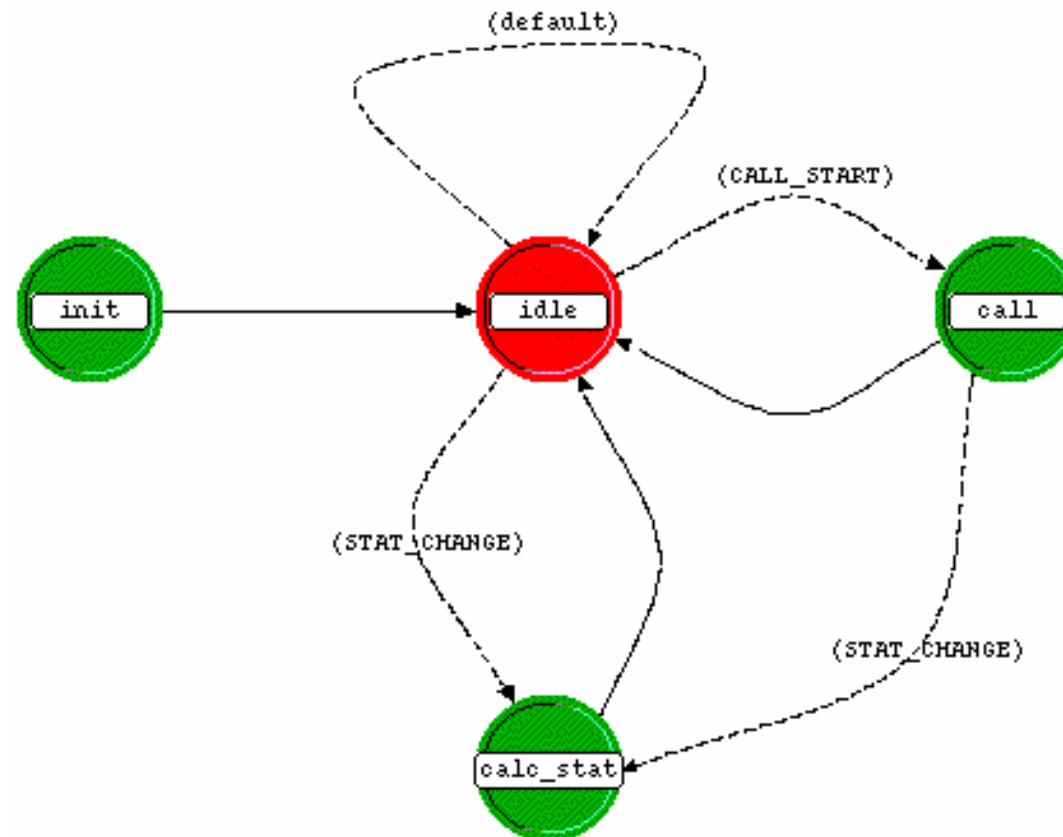
Central switch (site) model

- Reads the trace file
- Generates packets according to calls from trace file
 - one call = one packet
 - $\text{packet_size (bits)} = k \times \text{call_duration (s)}$
 - k: bit rate of channels (k=1,000 bps in simulations)
- Checks for availability of channels in the cells and sending packets to appropriate cells
- Collects statistics

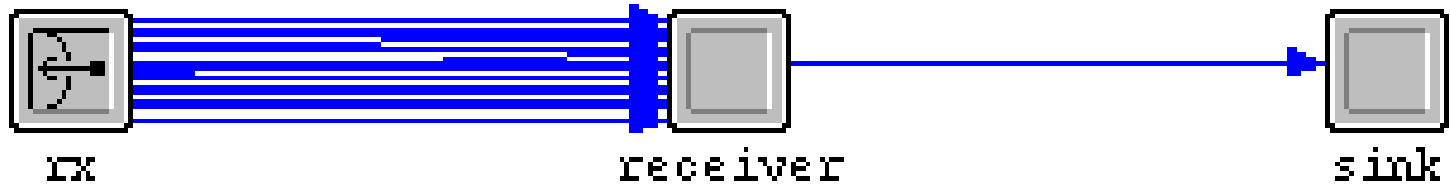
Central switch: OPNET node model



Dispatcher module in the central switch: OPNET process model



Cell: OPNET node model





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Statistical concepts

- Probability distribution:
 - probability that outcomes of a process are within a given range of values
 - expressed through **probability density (pdf)** and **cumulative distribution (cdf)** functions
- Autocorrelation:
 - measures the **dependence between two outcomes** of a process
 - wide-sense stationary processes: autocorrelation depends only on the difference (**lag**) between the time instances of the outcomes



Long-range dependence: definition

- Slow decay of the autocorrelation function $r(k)$ of a (wide-sense) stationary process $X(n)$:

$$\sum_{k=-\infty}^{\infty} r(k) = \infty$$

definition

$$r(k) = c_r k^{-(2-2H)}, \quad k \rightarrow \infty$$

model

$$f(v) = c_f |v|^{-\alpha}, \quad v \rightarrow 0$$

corollary

where $f(v)$ is the power spectral density of $X(n)$,
 c_r and c_f are non-zero constants, and $0 < \alpha < 1$

$0.5 < H < 1$ implies LRD

LRD: long-range dependence



Wavelet coefficients

- Discrete wavelet transform of a signal $X(t)$:

$$d(j, k) = \int_{-\infty}^{\infty} X(t) \psi_{j,k}(t) dt \quad \text{wavelet coefficients}$$

where

$$\psi_{j,k}(t) = 2^{-j/2} \psi(2^{-j}t - k)$$

- $\psi(t)$: mother wavelet
 - j : octave
 - k : translation

- Reconstruction formula:

$$X(t) = \sum_{j=0}^{\infty} \sum_k d(j, k) \psi_{j,k}(t)$$



LRD and wavelets

- Let $X(t)$ be LRD process (wide-sense stationary)
 - its power spectral density:

$$f(\nu) \sim c_f |\nu|^{-\alpha}, \nu \rightarrow 0$$

- Mean square value of its wavelet coefficients on octave j satisfies:

$$E\{d(j, k)^2\} = 2^{j\alpha} c_f C(\alpha, \psi)$$

where $C(\alpha, \psi) = \int |\nu|^{-\alpha} |\Psi(\nu)|^2 d\nu$ does not depend on j

D. Veitch and P. Abry, "A wavelet-based joint estimator of the parameters of long-range dependence," *IEEE Trans. on Information Theory*, vol. 45, no. 3, pp. 878–897, Apr. 1999.



LRD and wavelets

- Logarithm:

$$\log_2 E\{d(j,k)^2\} = \alpha \times j + c$$

- Important property: for given j , $d(j,k)$ does not exhibit long-range dependence (with respect to k)
 - with appropriately chosen mother wavelet

- Hence:

- simple estimator for $E\{d(j,k)^2\}$ is a sample mean:

$$E\{d(j,k)^2\} = \frac{1}{n_j} \sum_{k=1}^{n_j} d(j,k)^2$$

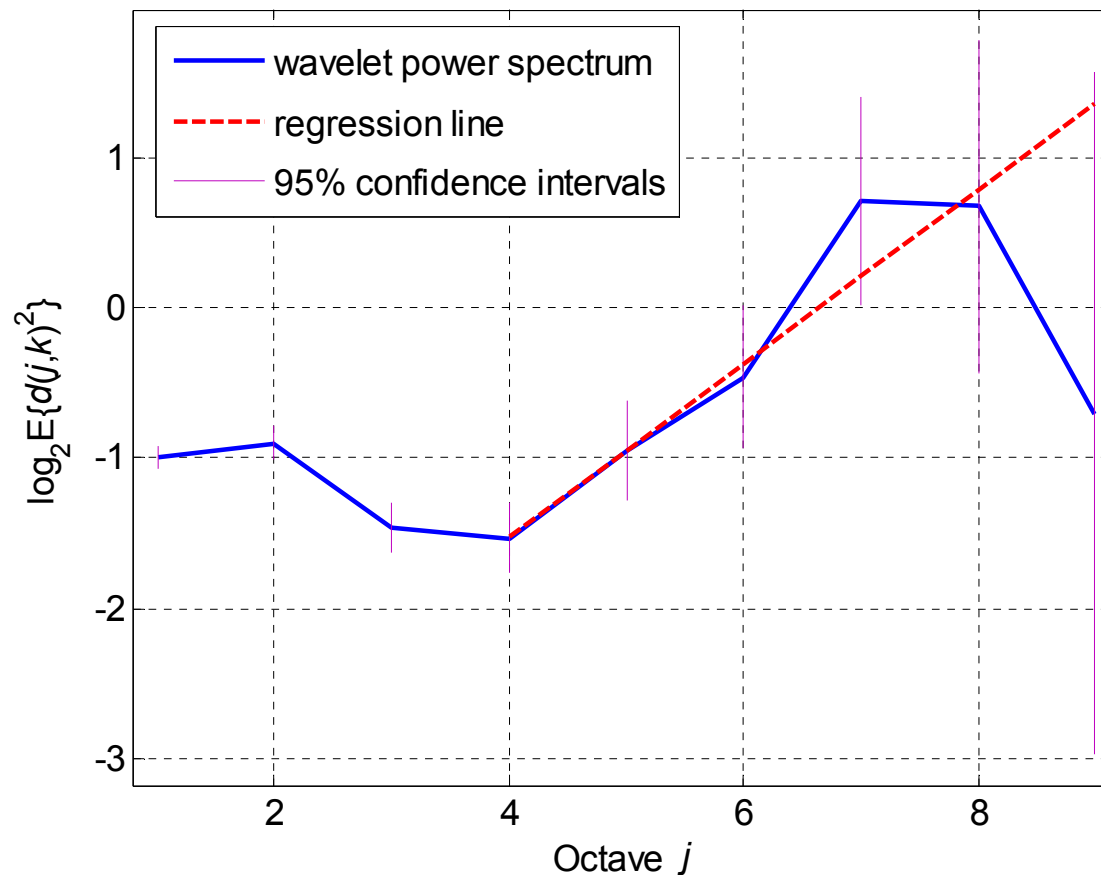
- n_j : number of wavelet coefficients at octave j



Estimation of α and H

- Logscale diagram: plot of $\log_2 E\{d(j,k)^2\}$ vs. j (octave)
- Linear relationship between $\log_2 E\{d(j,k)^2\}$ and j on the coarsest octaves indicates **LRD**
- Estimation of α :
 - linear regression of $\log_2 E\{d(j,k)^2\}$ on j in the linear region of the logscale diagram
- $H = 0.5 (\alpha + 1)$

Logscale diagram: example



- call inter-arrival times: 22:00–23:00, 26.03.2003
- $\alpha=0.576$, $H=0.788$ (octaves 4–9)



Test for time constancy of α

- $X(n)$: wide-sense stationary process
 - α does not depend on n
- Is α constant throughout the time series $X(n)$?
- Approach:
 - divide $X(n)$ into m blocks of equal length
 - estimate α for each block
 - compare the estimates
- If α varies significantly, estimating α for the entire time series is not meaningful
- In our analysis: $m \in \{3, 4, 5, 6, 7, 8, 10\}$



Kolmogorov-Smirnov test

- Goodness-of-fit test: quantitative decision whether the empirical cumulative distribution function (ECDF) of a set of observations is consistent with a random sample from an assumed theoretical distribution
- ECDF is a step function (step size $1/N$) of N ordered data points Y_1, Y_2, \dots, Y_N :

$$E_N = \frac{n(i)}{N}$$

$n(i)$: the number of data samples with values smaller than Y_i



Parameters

- Hypothesis:
 - null: the candidate distribution **fits** the empirical data
 - alternative: the candidate distribution **does not fit** the empirical data
- Input parameters: **significance level σ** and **tail**
- Output parameters:
 - **p-value**
 - **k: test statistic**
 - **cv: critical (cut-off) value**



Input parameters

- **Significance level σ** : determines if the null hypothesis is wrongly rejected σ percent of times, if it is in fact true
 - default value $\sigma = 0.05$
- σ defines sensitivity of the test:
 - smaller σ implies larger **critical value** (larger tolerance)
- **tail**: specifies whether the K-S performs two sided test (default) or tests from one or other side of the candidate distribution



Output parameters

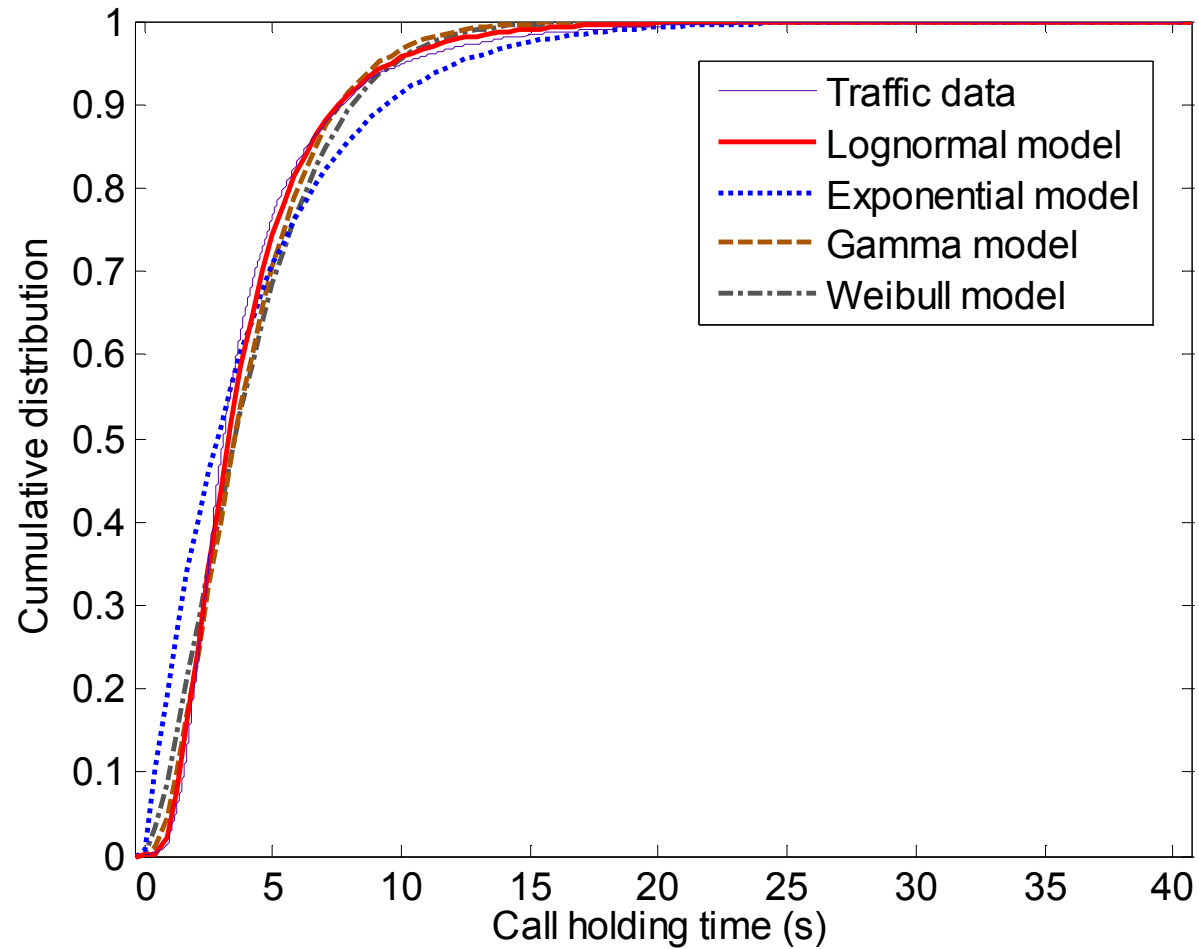
- Test statistic k is the maximum difference over all data points:

$$k = \max_{1 \leq i \leq N} \left| F(Y_i) - \frac{i}{N} \right|$$

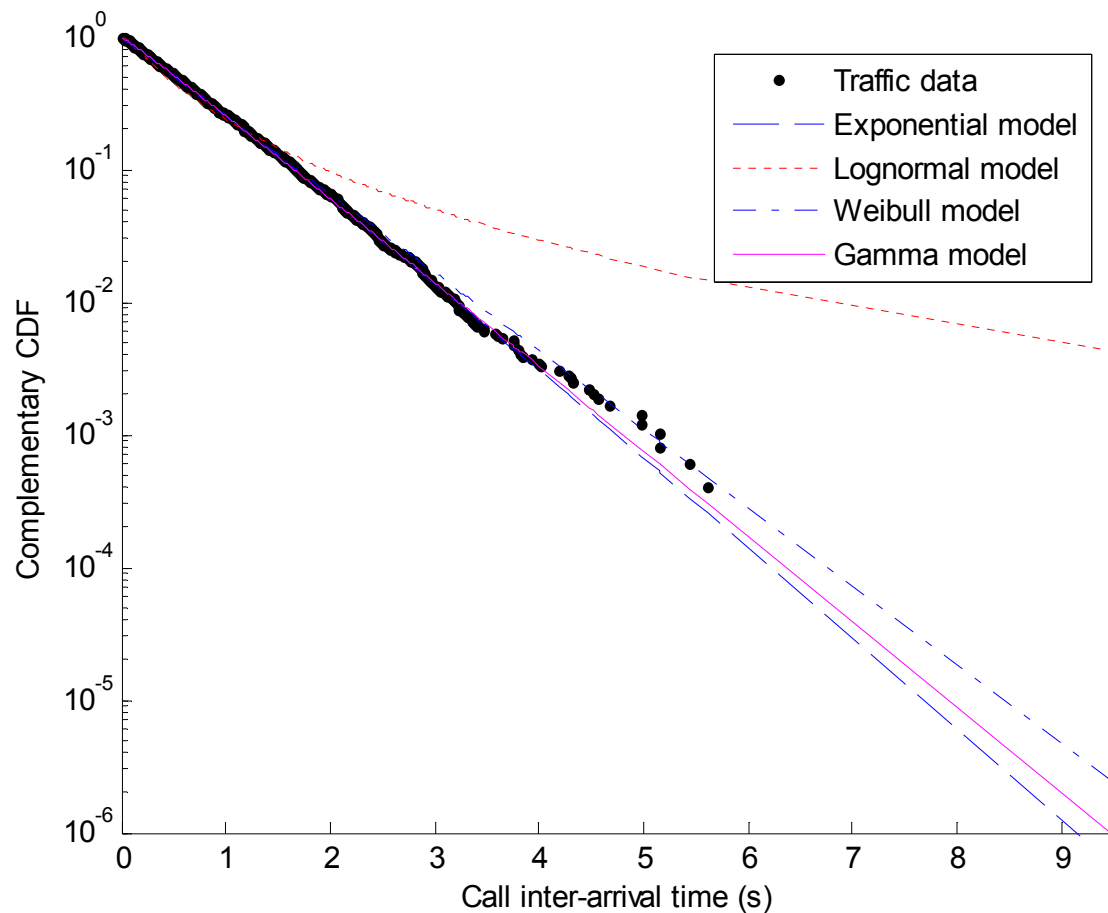
where F is the CDF of the assumed distribution

- The null hypothesis is accepted if the value of the test statistic is smaller than the critical value
- p-value is probability level when the difference between distributions (test statistics) becomes significant:
 - if p-value $\leq \sigma$: test rejects the null hypothesis
- If test returns critical value = NaN, the decision to accept or reject null hypothesis is based only on p-value

Best-fitting distributions: CDF



Inter-arrival time: complementary CDF



K-S test: call inter-arrival times 2001

Significance level $\sigma = 0.1$

| Distribution | Parameter | 02.11.2001, 20:00–21:00 | 02.11.2001, 16:00–17:00 | 02.11.2001, 15:00–16:00 | 01.11.2001, 19:00–20:00 | 01.11.2001, 00:00–01:00 |
|--------------|-----------|----------------------------|----------------------------|----------------------------|----------------------------|----------------------------|
| exponential | h | 1 | 1 | 0 | 1 | 1 |
| | p | 0.0384 | 0.0001 | 0.5416 | 0.0122 | 0.0135 |
| | k | 0.0247 | 0.0369 | 0.0131 | 0.0277 | 0.0259 |
| Weibull | h | 0 | 1 | 0 | 0 | 1 |
| | p | 0.3036 | 0.0409 | 0.4994 | 0.1574 | 0.0837 |
| | k | 0.0171 | 0.0236 | 0.0136 | 0.0195 | 0.0206 |
| gamma | h | 0 | 1 | 0 | 1 | 1 |
| | p | 0.3833 | 0.0062 | 0.3916 | 0.0644 | 0.0953 |
| | k | 0.0159 | 0.0287 | 0.0148 | 0.0227 | 0.0202 |

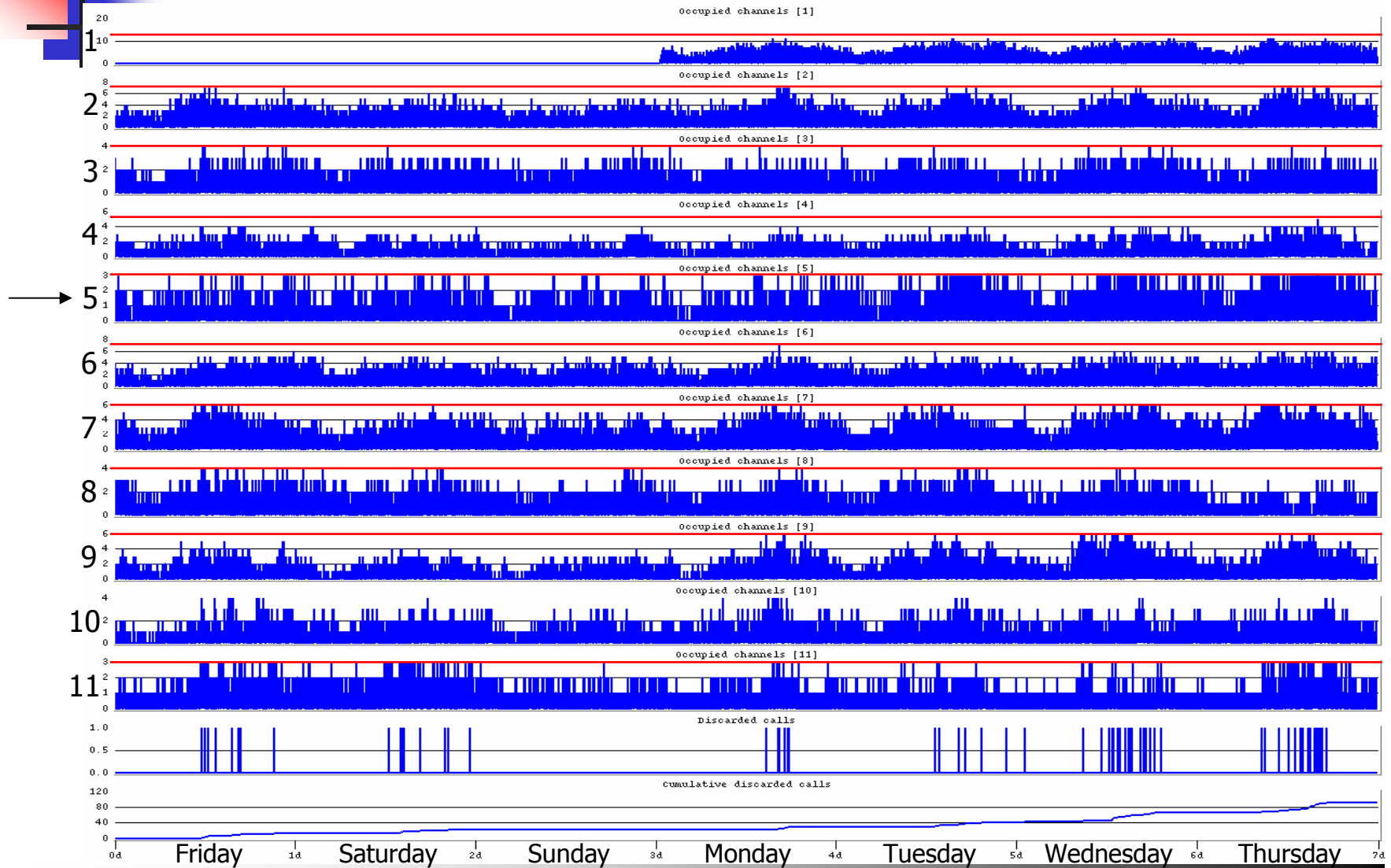
| Significance level σ | 0.01 | 0.04 | 0.05 | 0.08 | 0.09 | 0.1 |
|-----------------------------|--------|--------|--------|--------|--------|--------|
| 02.11.2001, 16:00–17:00: cv | 0.0275 | 0.0237 | 0.0230 | 0.0215 | 0.0211 | 0.0207 |
| 01.11.2001, 00:00–01:00: cv | 0.0267 | 0.0229 | 0.0223 | 0.0208 | 0.0204 | 0.0201 |



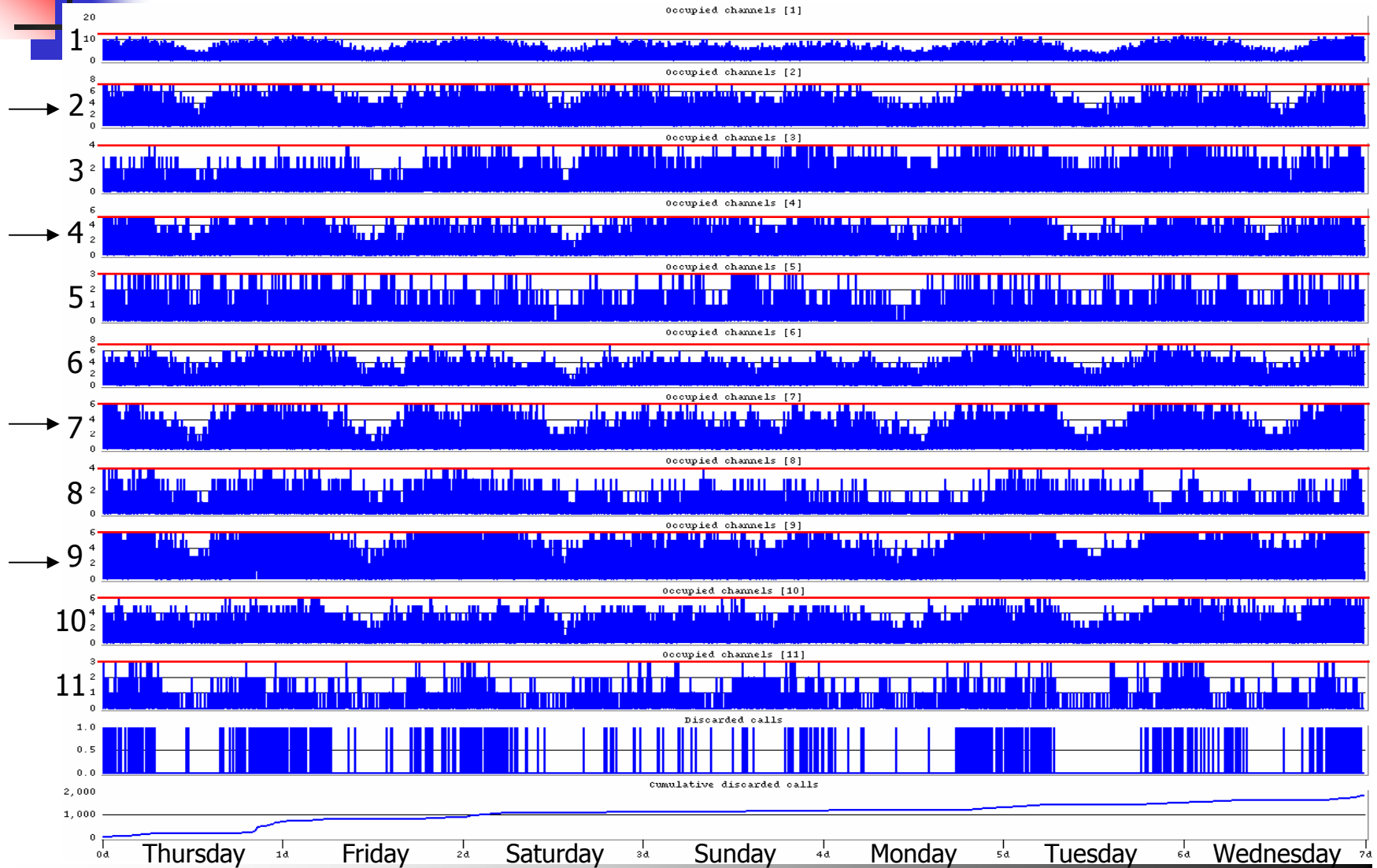
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Simulation results: 2002



Simulation results: 2003





Observations

- Presence of daily cycles:
 - minimum utilization: \sim 2 PM
 - maximum utilization: 9 PM – 3 AM
- 2002 sample data:
 - cell 5 is the busiest
 - other cells seldom reach their capacities
- 2003 sample data:
 - several cells (2, 4, 7, and 9) have all channels occupied during busy hours

Discarded calls

- appear only in the OPNET simulation results (do not exist in the deployed network)
- occur during busy hours
- may be used to identify possibly congested cells

| Sample data | Cell no. | Capacity | No. of discarded calls |
|-------------|----------|----------|------------------------|
| 2002 | | original | 91 |
| 2002 | 5 | 3 + 1 | 62 |
| 2003 | | original | 1,812 |
| 2003 | 9 | 6 + 1 | 679 |
| 2003 | 4 | 5 + 1 | 521 |
| | 9 | 6 + 1 | |

| original cap. | |
|---------------|-----|
| cell | ch. |
| 1 | 12 |
| 2 | 7 |
| 3 | 4 |
| 4 | 5 |
| 5 | 3 |
| 6 | 7 |
| 7 | 6 |
| 8 | 4 |
| 9 | 6 |
| 10 | 6 |
| 11 | 3 |



Maximum and average utilizations

| Cell | Capacity | 2002 | | 2003 | |
|------|----------|---------|---------|---------|---------|
| | | Maximum | Average | Maximum | Average |
| 1 | 12 | 11 | 2.5 | 11 | 2.6 |
| 2 | 7 | 7 | 0.8 | 7 | 1.6 |
| 3 | 4 | 4 | 0.3 | 4 | 0.5 |
| 4 | 5 | 5 | 0.3 | 5 | 1.1 |
| 5 | 3 | 3 | 0.2 | 3 | 0.3 |
| 6 | 7 | 7 | 0.7 | 7 | 1.2 |
| 7 | 6 | 6 | 0.7 | 6 | 1.1 |
| 8 | 4 | 4 | 0.3 | 4 | 0.4 |
| 9 | 6 | 6 | 0.4 | 6 | 1.6 |
| 10 | 6 | 4 | 0.2 | 6 | 1.0 |
| 11 | 3 | 3 | 0.2 | 3 | 0.2 |



General OPNET statistics for data samples

- 2002 sample data:
 - span: 8:00, February 1 – 8:00, February 8
 - number of calls: 403,590
 - discarded calls: 91
- 2003 sample data
 - span: 0:00, March 20–24:00, March 26
 - number of calls: 645,167
 - discarded calls: 1,812
- Discarded calls are due to discrepancies in the data
 - they appear only in simulation results



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Statistical distributions

- Fourteen candidate distributions:
 - exponential, Weibull, gamma, normal, lognormal, logistic, log-logistic, Nakagami, Rayleigh, Rician, t-location scale, Birnbaum-Saunders, extreme value, inverse Gaussian
- Parameters of the distributions: calculated by performing maximum likelihood estimation
- Best fitting distributions are determined by:
 - visual inspection of the distribution of the trace and the candidate distributions
 - K-S test on potential candidates



Maximum Likelihood Estimation (MLE)

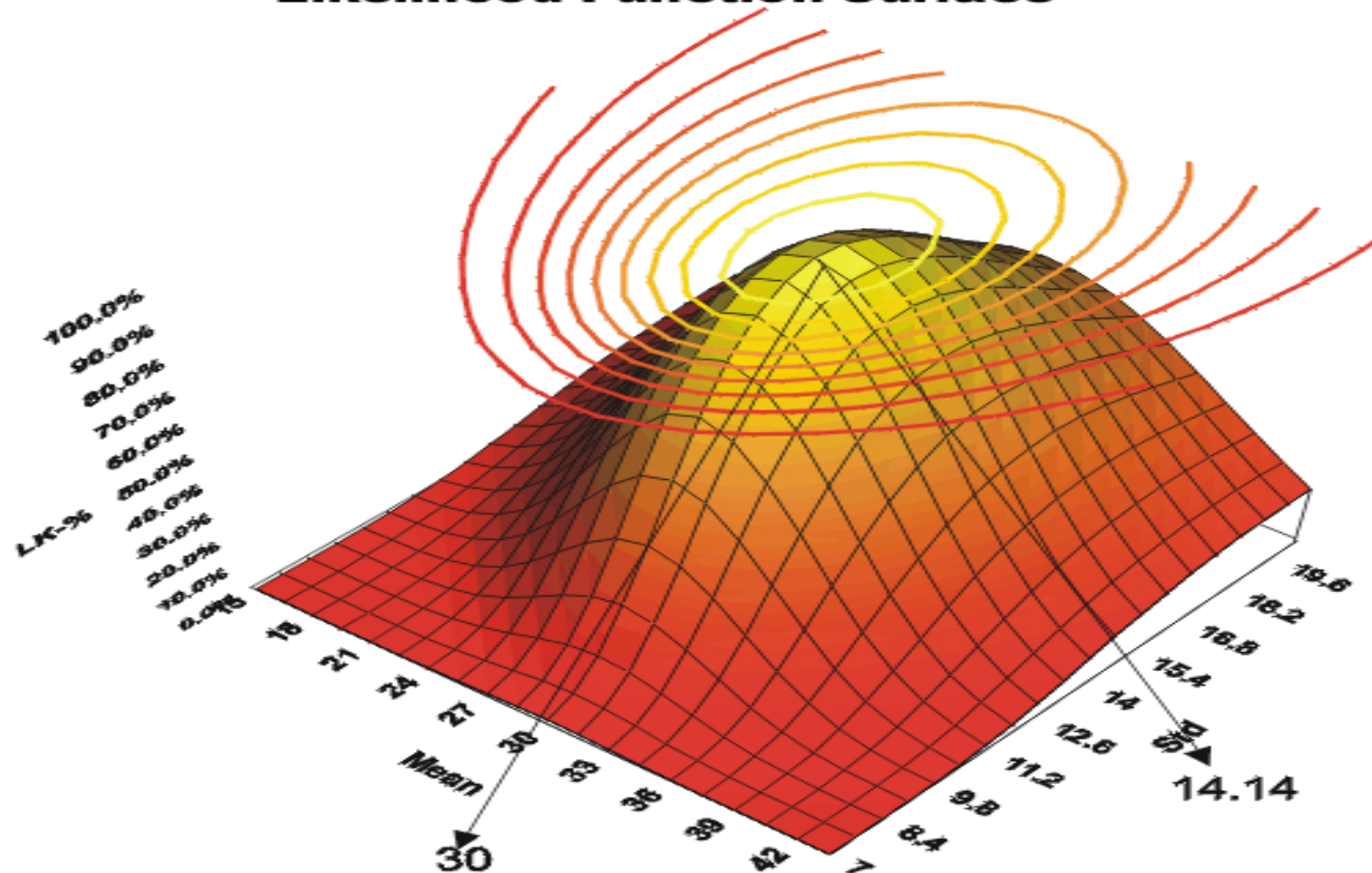
- Introduced by R. A. Fisher in 1920s
- The most popular method for parameter estimation
- Goal: to find the distribution parameters that make the given distribution that follow the most closely underlying data set
- Conduct an experiment and obtain N independent observations
- $\theta_1, \theta_2, \dots, \theta_k$ are k unknown constant parameters which

$$L(x_1, x_2, \dots, x_N | \theta_1, \theta_2, \dots, \theta_k) = L = \prod_{i=1}^N f(x_i; \theta_1, \theta_2, \dots, \theta_k)$$

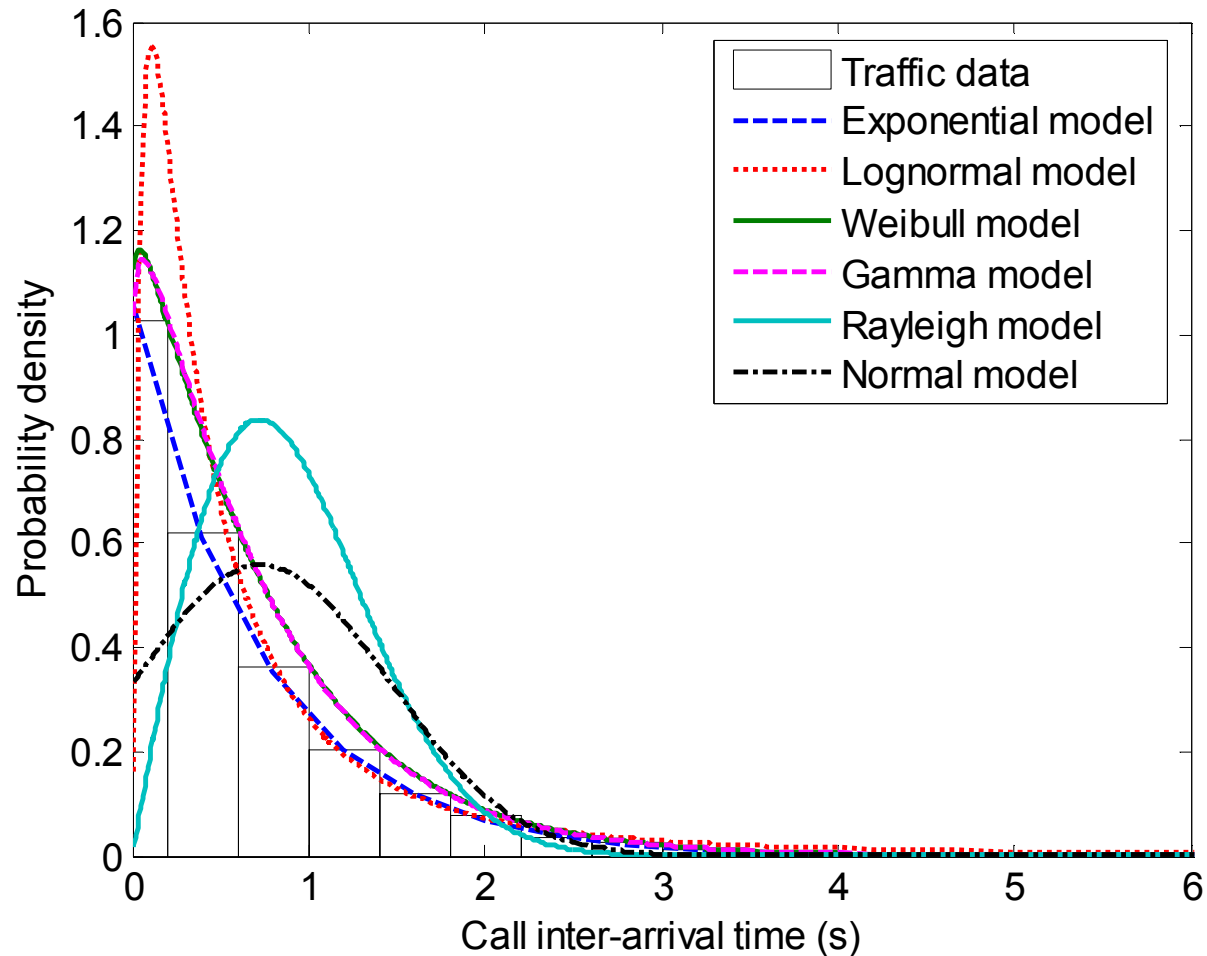
$i = 1, 2, \dots, N$

Maximum likelihood estimation

Likelihood Function Surface



Call inter-arrival times: pdf candidates

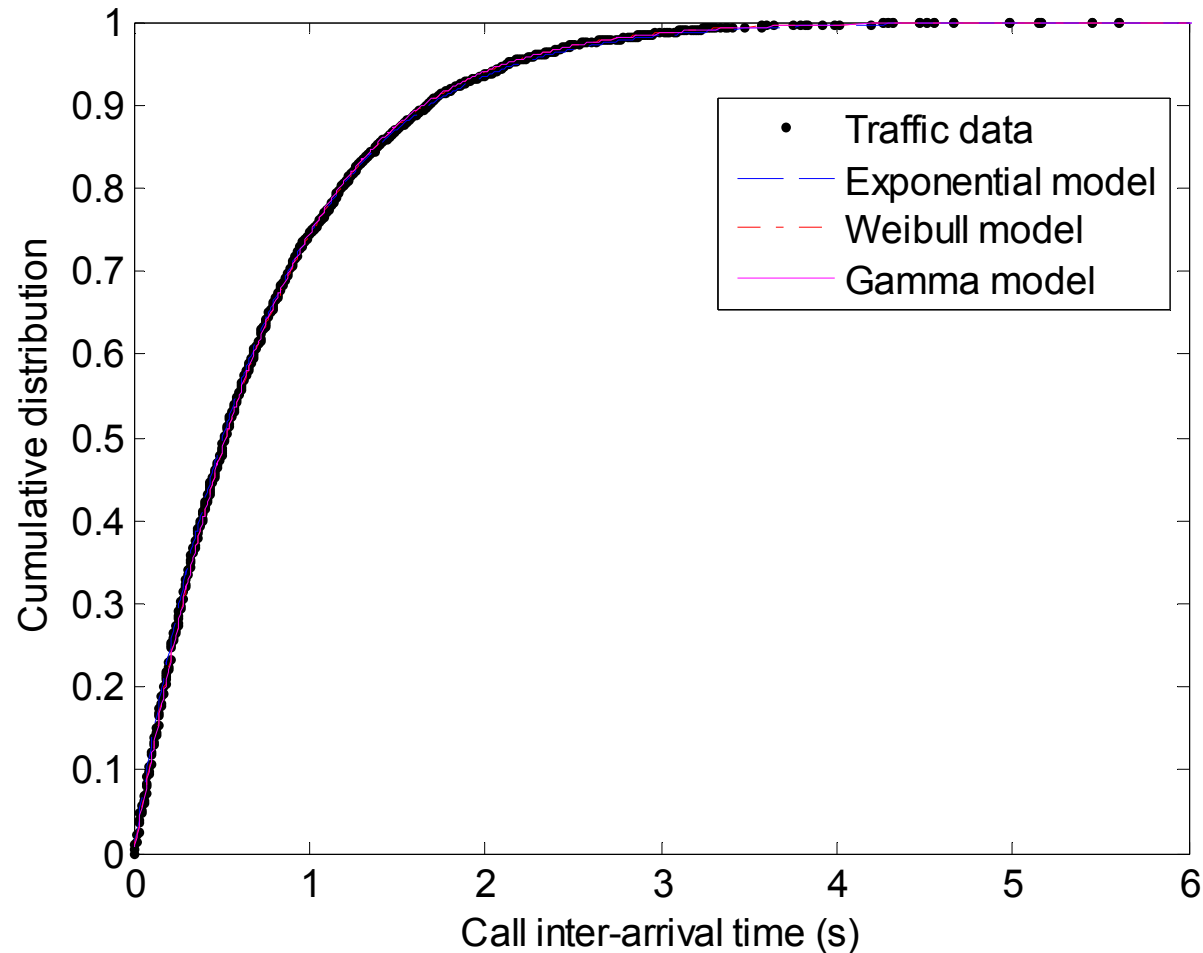




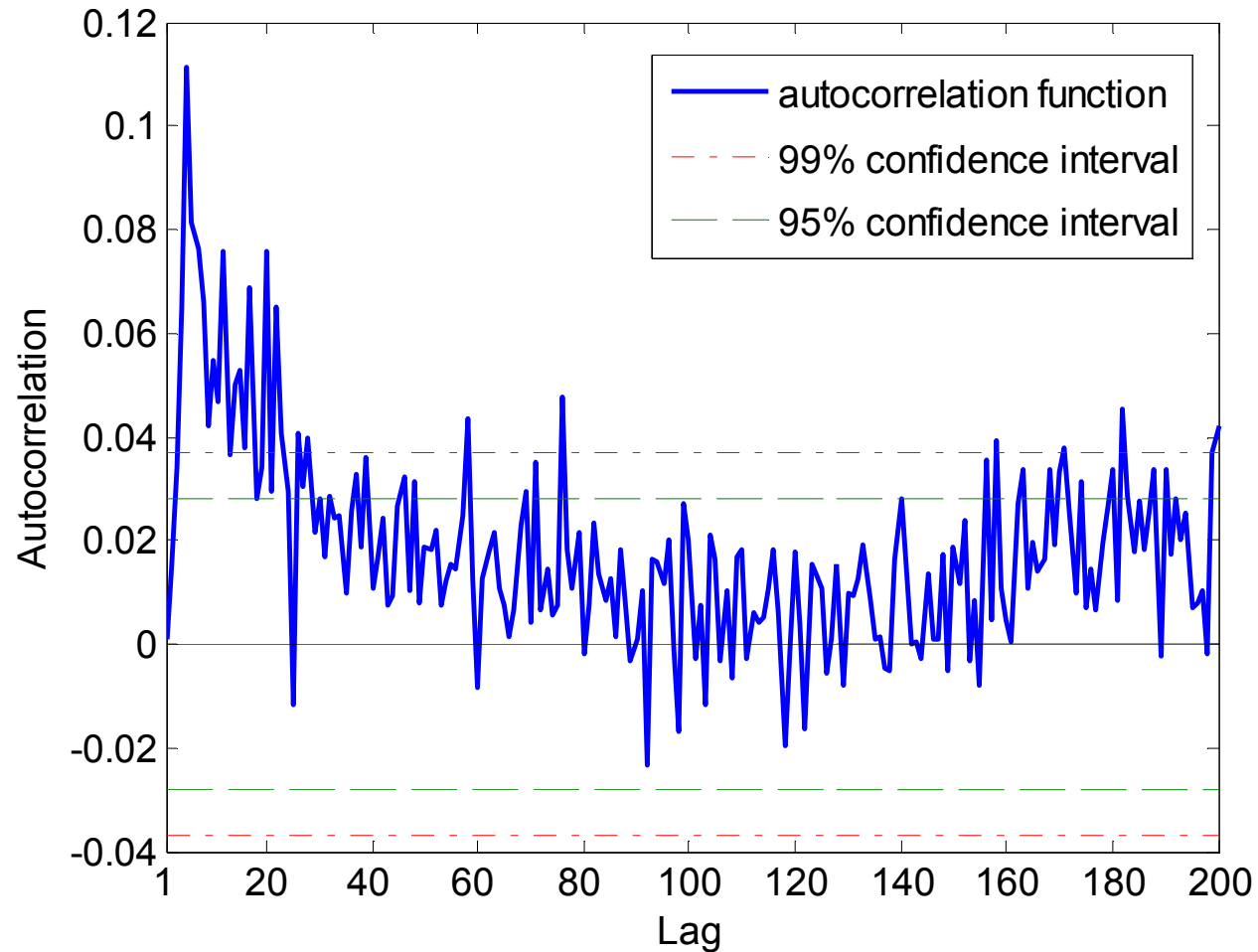
K-S test results: 2003

| Distribution | Parameter | 26.03.2003, 22:00–23:00 | 25.03.2003, 23:00–24:00 | 26.03.2003, 23:00–24:00 | 29.03.2003, 02:00–03:00 | 29.03.2003, 01:00–02:00 |
|--------------|-----------|----------------------------|----------------------------|----------------------------|----------------------------|----------------------------|
| Exponential | h | 1 | 1 | 0 | 1 | 1 |
| | p | 0.0027 | 0.0469 | 0.4049 | 0.0316 | 0.1101 |
| | k | 0.0283 | 0.0214 | 0.0137 | 0.0205 | 0.0185 |
| Weibull | h | 0 | 0 | 0 | 0 | 0 |
| | p | 0.4885 | 0.4662 | 0.2065 | 0.286 | 0.2337 |
| | k | 0.013 | 0.0133 | 0.0164 | 0.014 | 0.0159 |
| Gamma | h | 0 | 0 | 0 | 0 | 0 |
| | p | 0.3956 | 0.3458 | 0.127 | 0.145 | 0.1672 |
| | k | 0.0139 | 0.0146 | 0.0181 | 0.0163 | 0.0171 |
| Lognormal | h | 1 | 1 | 1 | 1 | 1 |
| | p | 1.015E-20 | 4.717E-15 | 2.97E-16 | 3.267E-23 | 4.851E-21 |
| | k | 0.0689 | 0.0629 | 0.0657 | 0.0795 | 0.0761 |

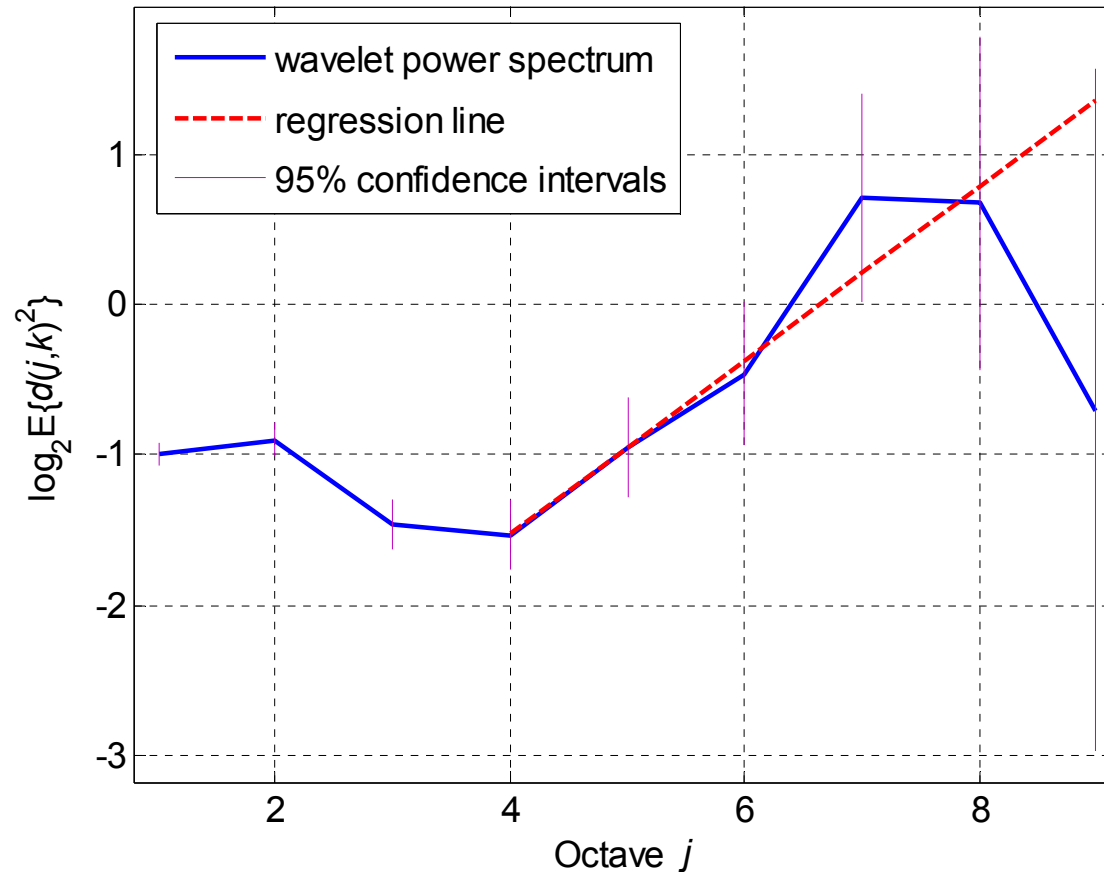
Call inter-arrival times: best-fitting distributions (cdf)



Call inter-arrival time: autocorrelation



Call inter-arrival times: 26.03.2003, 22:00–23:00



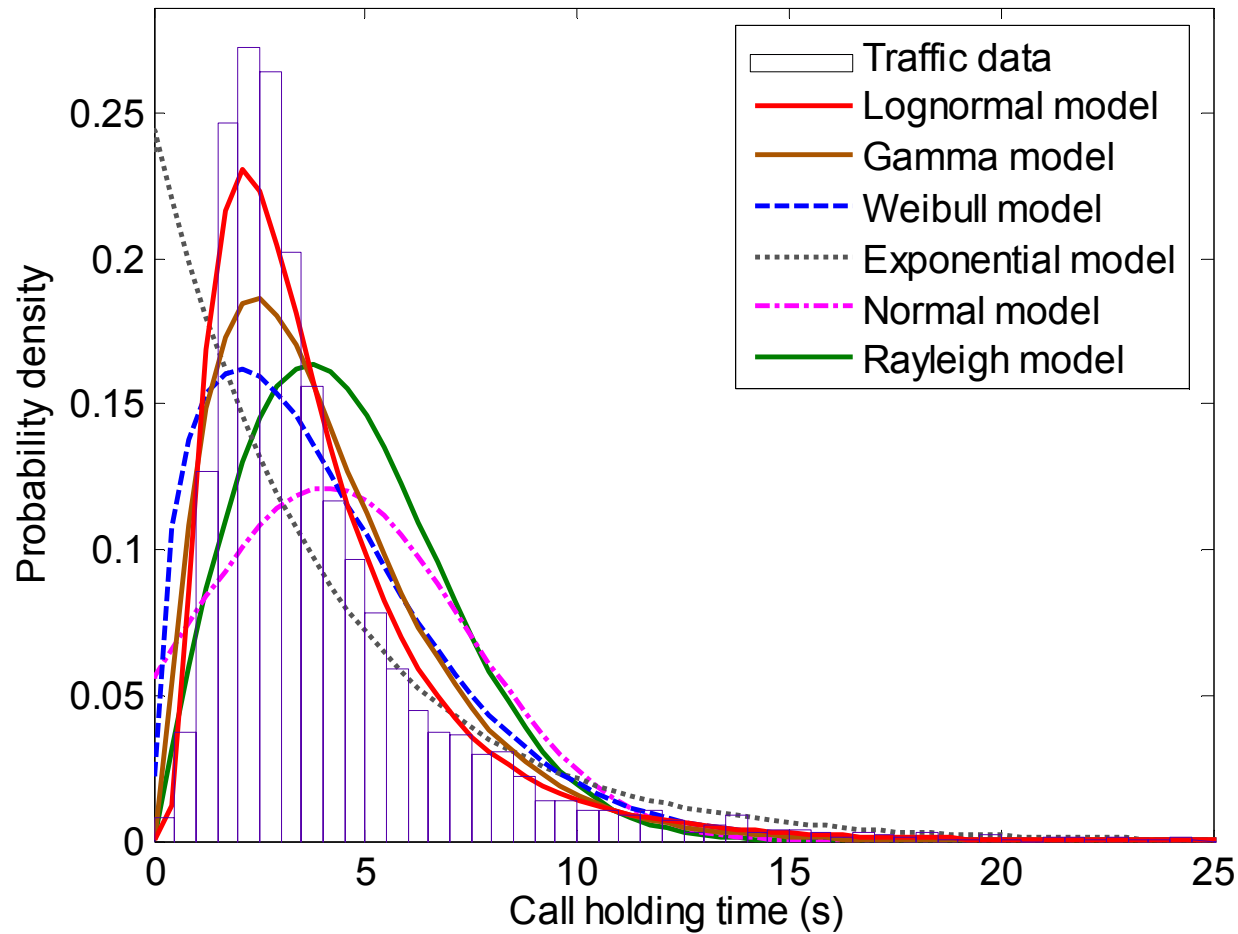
- **LRD:** $\alpha > 0$ ($H > 0.5$)
- other traces have similar logscale diagrams

Call inter-arrival times: estimates of H

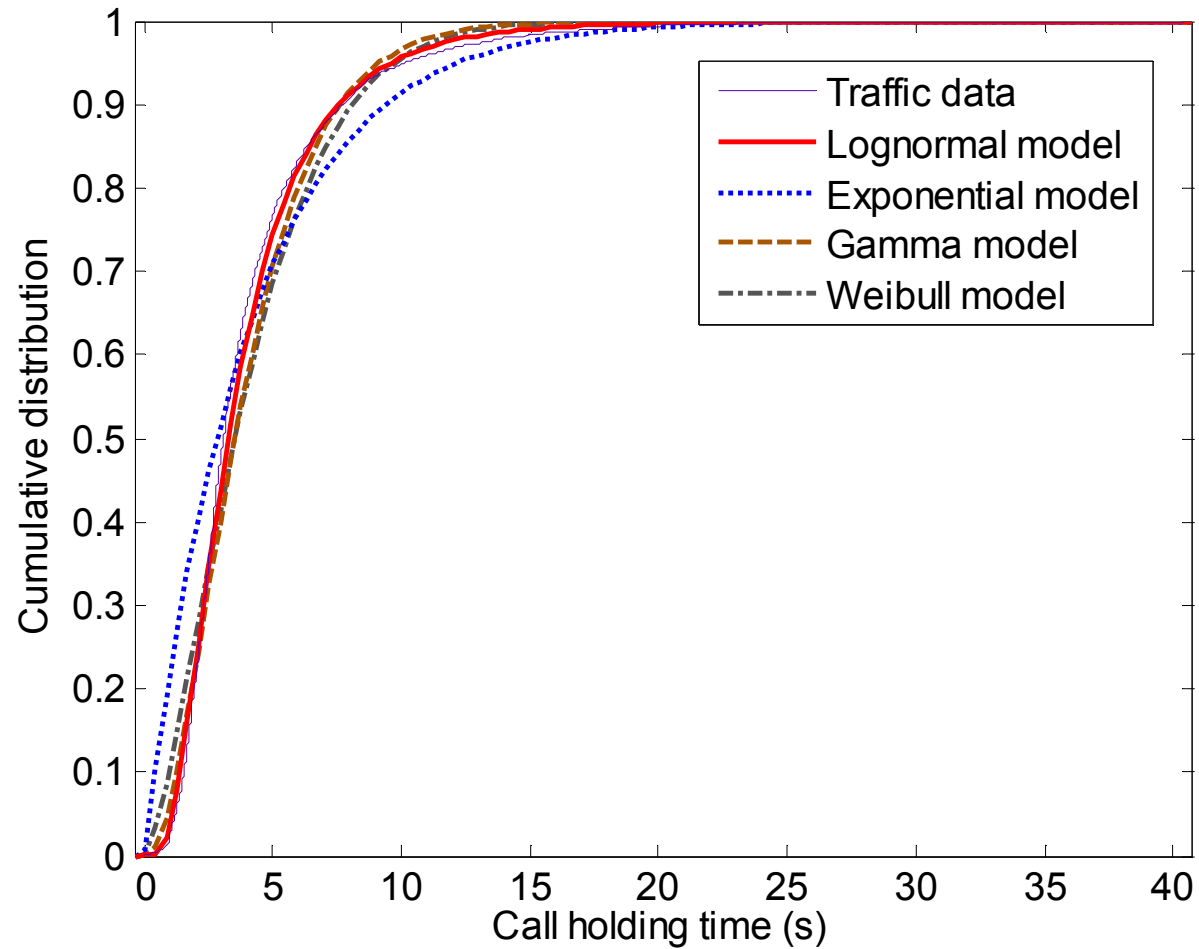
- Traces pass the test for time constancy of α : estimates of H are reliable

| 2001 | | 2002 | | 2003 | |
|---------------------------|-------|---------------------------|-------|---------------------------|-------|
| Day/hour | H | Day/hour | H | Day/hour | H |
| 02.11.2001 15:00–16:00 | 0.907 | 01.03.2002 04:00–05:00 | 0.679 | 26.03.2003 22:00–23:00 | 0.788 |
| 01.11.2001 00:00–01:00 | 0.802 | 01.03.2002 22:00–23:00 | 0.757 | 25.03.2003 23:00–24:00 | 0.832 |
| 02.11.2001 16:00–17:00 | 0.770 | 01.03.2002 23:00–24:00 | 0.780 | 26.03.2003 23:00–24:00 | 0.699 |
| 01.11.2001 19:00–20:00 | 0.774 | 01.03.2002 00:00–01:00 | 0.741 | 29.03.2003 02:00–03:00 | 0.696 |
| 02.11.2001 20:00–21:00 | 0.663 | 02.03.2002 00:00–01:00 | 0.747 | 29.03.2003 01:00–02:00 | 0.705 |

Call holding time: pdf candidates



Best-fitting distributions: cdf

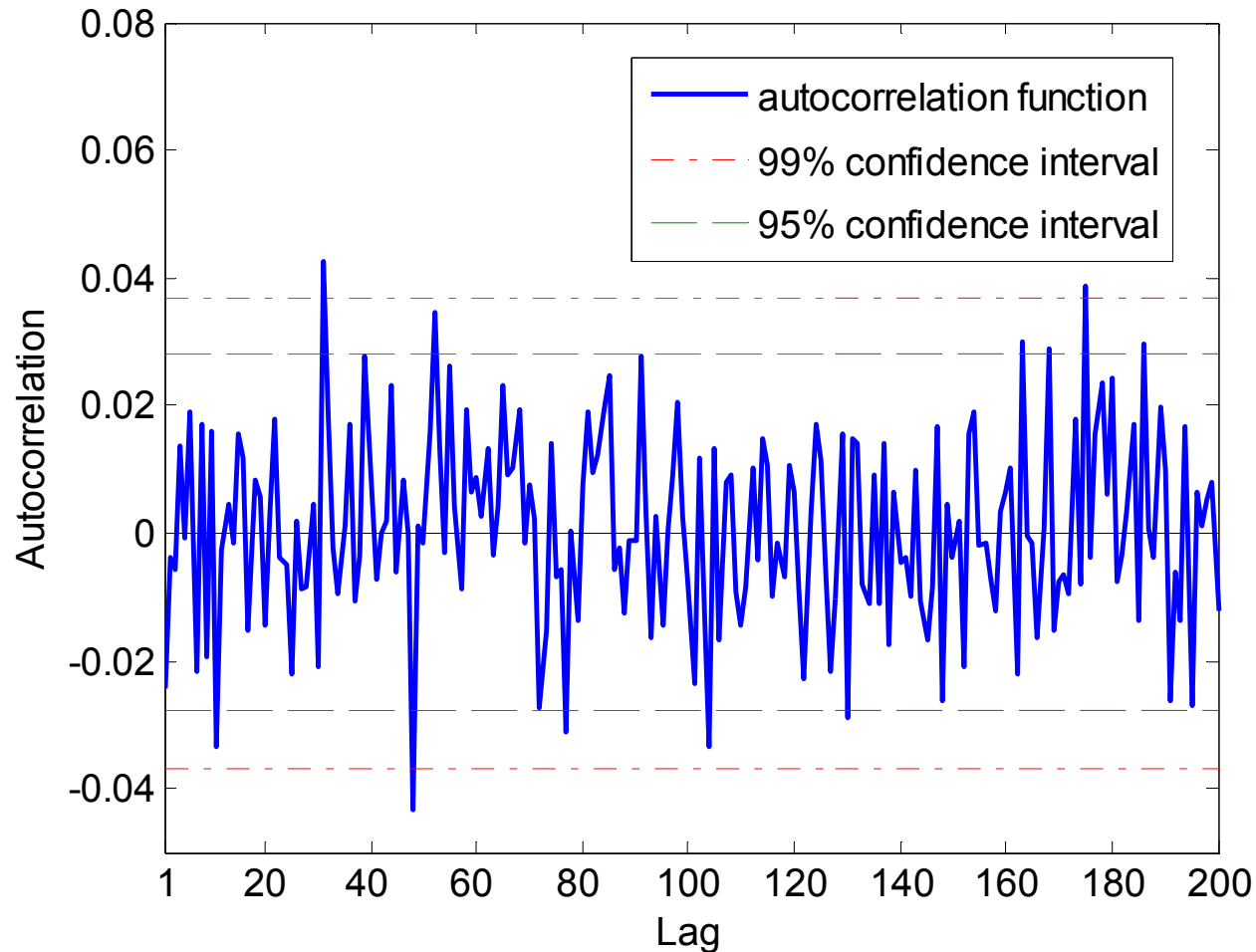




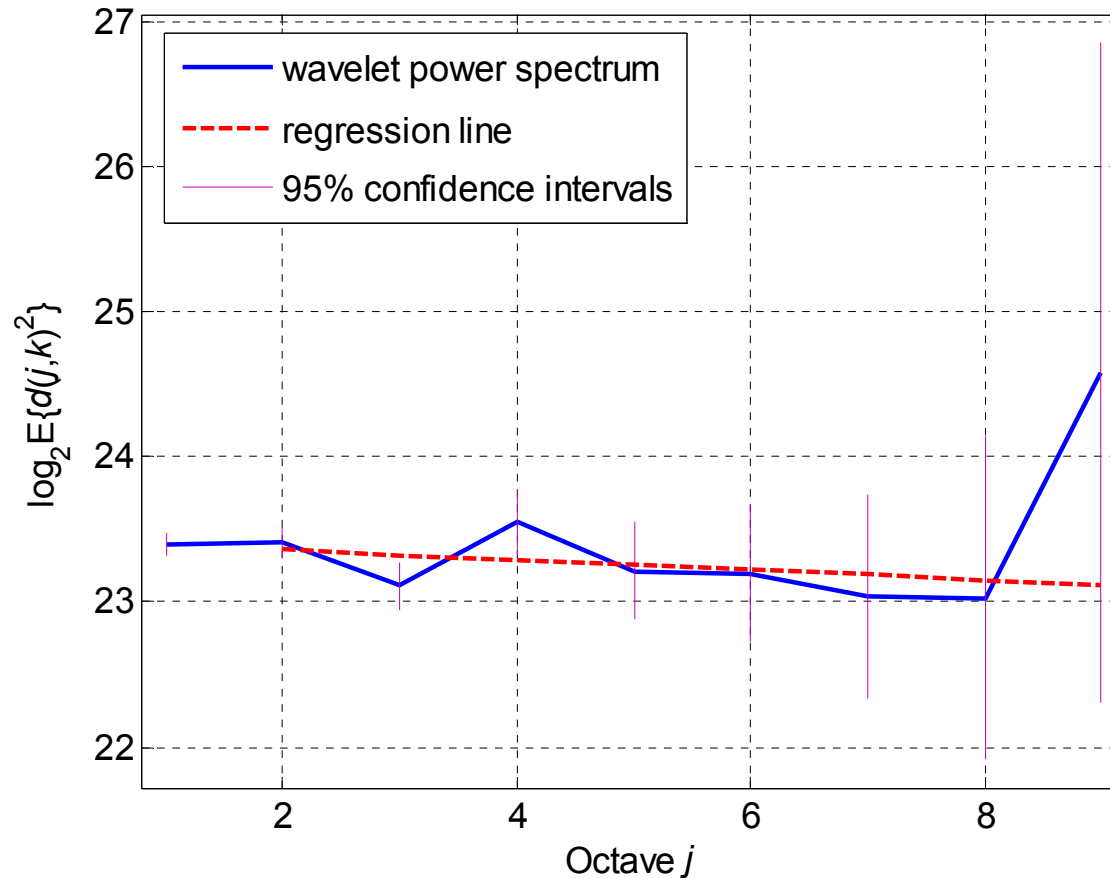
K-S test results: 2003

- No distribution passes the test when the entire trace is tested (significance levels = 0.1 and 0.01)
- Lognormal distribution passes test (significance level = 0.01) for:
 - 5-6 sub-traces from 15 randomly chosen 1,000-sample sub-traces
 - passes the test for almost all 500-sample sub-traces
- Test rejects null hypothesis when the sub-traces are compared with candidate distributions:
 - exponential
 - Weibull
 - gamma

Call holding time: autocorrelation



Logscale diagram, call holding times: 26.03.2003, 22:00–23:00



- **independence:** $\alpha \approx 0$ ($H \approx 0.5$)
- other traces have similar logscale diagrams

Call holding times: estimates of H

- all traces (except one) pass the test for constancy of α
- only one unreliable estimate (*): consistent value

| 2001 | | 2002 | | 2003 | |
|---------------------------|-------|---------------------------|-------|---------------------------|-------|
| Day/hour | H | Day/hour | H | Day/hour | H |
| 02.11.2001 15:00–16:00 | 0.493 | 01.03.2002 04:00–05:00 | 0.490 | 26.03.2003 22:00–23:00 | 0.483 |
| 01.11.2001 00:00–01:00 | 0.471 | 01.03.2002 22:00–23:00 | 0.460 | 25.03.2003 23:00–24:00 | 0.483 |
| 02.11.2001 16:00–17:00 | 0.462 | 01.03.2002 23:00–24:00 | 0.489 | 26.03.2003 23:00–24:00 | * |
| 01.11.2001 19:00–20:00 | 0.467 | 01.03.2002 00:00–01:00 | 0.508 | 29.03.2003 02:00–03:00 | 0.526 |
| 02.11.2001 20:00–21:00 | 0.479 | 02.03.2002 00:00–01:00 | 0.503 | 29.03.2003 01:00–02:00 | 0.466 |

Call inter-arrival and call holding times

| | 2001 | | 2002 | | 2003 | |
|---------------|-------------|----------|-------------|----------|-------------|----------|
| | Day/hour | Avg. (s) | Day/hour | Avg. (s) | Day/hour | Avg. (s) |
| inter-arrival | 02.11.2001 | 0.97 | 01.03.2002 | 0.81 | 26.03.2003 | 0.73 |
| holding | 15:00–16:00 | 3.78 | 04:00–05:00 | 4.07 | 22:00–23:00 | 4.08 |
| inter-arrival | 01.11.2001 | 0.97 | 01.03.2002 | 0.83 | 25.03.2003 | 0.85 |
| holding | 00:00–01:00 | 3.95 | 22:00–23:00 | 3.84 | 23:00–24:00 | 4.12 |
| inter-arrival | 02.11.2001 | 1.03 | 01.03.2002 | 0.86 | 26.03.2003 | 0.85 |
| holding | 16:00–17:00 | 3.99 | 23:00–24:00 | 3.88 | 23:00–24:00 | 4.04 |
| inter-arrival | 01.11.2001 | 1.09 | 01.03.2002 | 0.91 | 29.03.2003 | 0.87 |
| holding | 19:00–20:00 | 3.97 | 00:00–01:00 | 3.95 | 02:00–03:00 | 4.14 |
| inter-arrival | 02.11.2001 | 1.12 | 02.03.2002 | 0.91 | 29.03.2003 | 0.88 |
| holding | 20:00–21:00 | 3.84 | 00:00–01:00 | 4.06 | 01:00–02:00 | 4.25 |

Avg. call inter-arrival times: 1.08 s (2001), 0.86 s (2002), 0.84 s (2003)

Avg. call holding times: 3.91 s (2001), 3.96 s (2002), 4.13 s (2003)



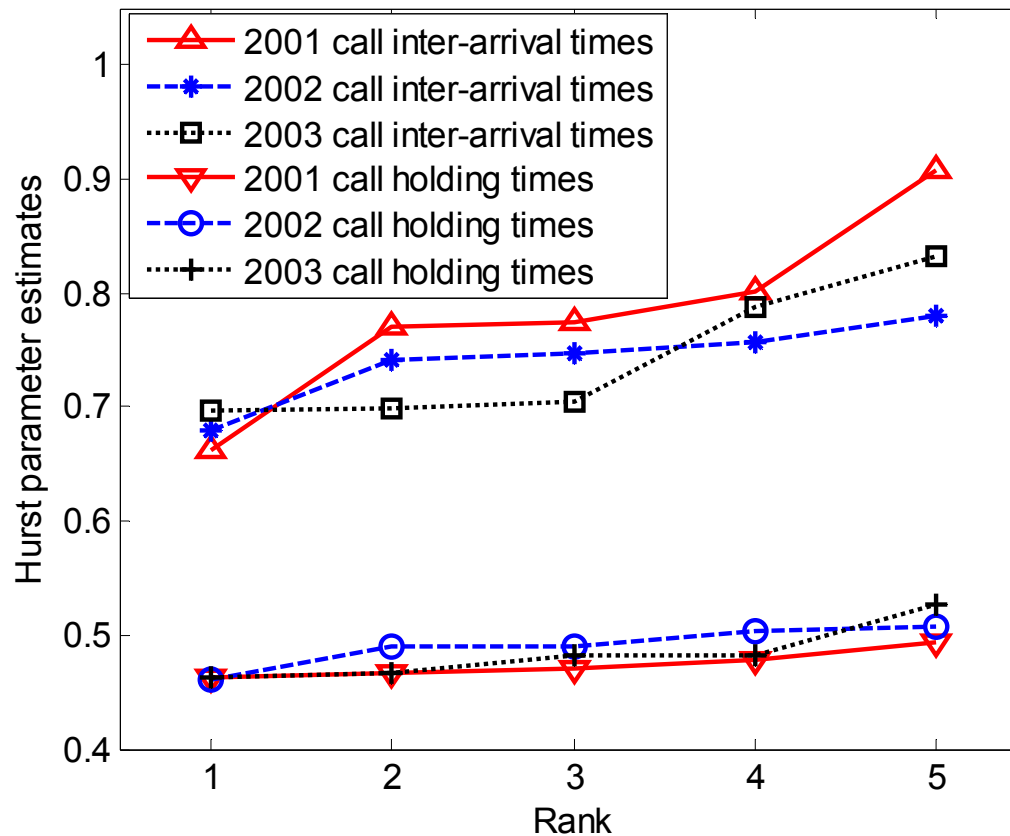
Distributions

| Distribution | Expression | Remark |
|--------------|--|--|
| exponential | $f(x) = \frac{e^{-x/\mu}}{\mu}$ | |
| Weibull | $f(x) = ba^{-b} x^{b-1} e^{-(x/a)^b} I_{(0,\infty)}(x)$ | $I_{(0,\infty)}(x)$: incomplete beta function |
| gamma | $f(x) = \frac{x^{a-1} e^{-(x/b)}}{b^a \Gamma(a)}$ | $\Gamma(a)$: gamma function |
| lognormal | $f(x) = \frac{e^{-\frac{(\ln x - \mu)^2}{2\sigma^2}}}{x\sigma\sqrt{2\pi}}$ | |

Best fitting distributions

| Busy hour | Distribution | | | | | |
|------------------------|--------------------------|--------|--------|--------|--------------------|----------|
| | Call inter-arrival times | | | | Call holding times | |
| | Weibull | | Gamma | | Lognormal | |
| | a | b | a | b | μ | σ |
| 02.11.2001 15:00–16:00 | 0.9785 | 1.1075 | 1.0326 | 0.9407 | 1.0913 | 0.6910 |
| 01.11.2001 00:00–01:00 | 0.9907 | 1.0517 | 1.0818 | 0.8977 | 1.0801 | 0.7535 |
| 02.11.2001 16:00–17:00 | 1.0651 | 1.0826 | 1.1189 | 0.9238 | 1.1432 | 0.6803 |
| 01.03.2002 04:00–05:00 | 0.8313 | 1.0603 | 1.1096 | 0.7319 | 1.1746 | 0.6671 |
| 01.03.2002 22:00–23:00 | 0.8532 | 1.0542 | 1.0931 | 0.7643 | 1.1157 | 0.6565 |
| 01.03.2002 23:00–24:00 | 0.8877 | 1.0790 | 1.1308 | 0.7623 | 1.1096 | 0.6803 |
| 26.03.2003 22:00–23:00 | 0.7475 | 1.0475 | 1.0910 | 0.6724 | 1.1838 | 0.6553 |
| 25.03.2003 23:00–24:00 | 0.8622 | 1.0376 | 1.0762 | 0.7891 | 1.1737 | 0.6715 |
| 26.03.2003 23:00–24:00 | 0.8579 | 1.0092 | 1.0299 | 0.8292 | 1.1704 | 0.6696 |

Estimates of H



- call inter-arrival times: $H \approx 0.7-0.8$
- call holding times: $H \approx 0.5$



Conclusions

- We created an OPNET model and simulated two weeks of network activity
- Network utilization exhibits daily cycles
- Between February 2002 and March 2003:
 - number of calls increased by $\sim 60\%$
 - average utilization increased non-uniformly across the network
- Several cells may become congested in future



Conclusions

- We analyzed **busy hours voice traffic** from a public safety wireless network in Vancouver, BC
 - call inter-arrival and call holding times during **five** busy hours from **2001, 2002, and 2003**
- Statistical distribution functions of traffic traces:
 - Kolmogorov-Smirnov goodness-of-fit test
 - autocorrelation functions
 - wavelet-based estimation of the Hurst parameter



Conclusions

- Call inter-arrival times:
 - best fit: Weibull and gamma distributions
 - long-range dependent: $H \approx 0.7-0.8$
- Call holding times:
 - best fit: lognormal distribution
 - uncorrelated



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